



University of
Strathclyde

Adaptive-window PMU algorithms using cascaded boxcar filters to meet and exceed C37.118.1(a) requirements

Dr. Andrew Roscoe



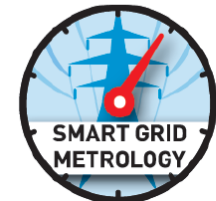
EMRP

European Metrology Research Programme
■ Programme of EURAMET

The EMRP is jointly funded by the EMRP participating countries
within EURAMET and the European Union



ENG52 SmartGrid II



Contributors to recent and forthcoming work



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C37.118.1a-2014

IEC/IEEE 60255-118-1



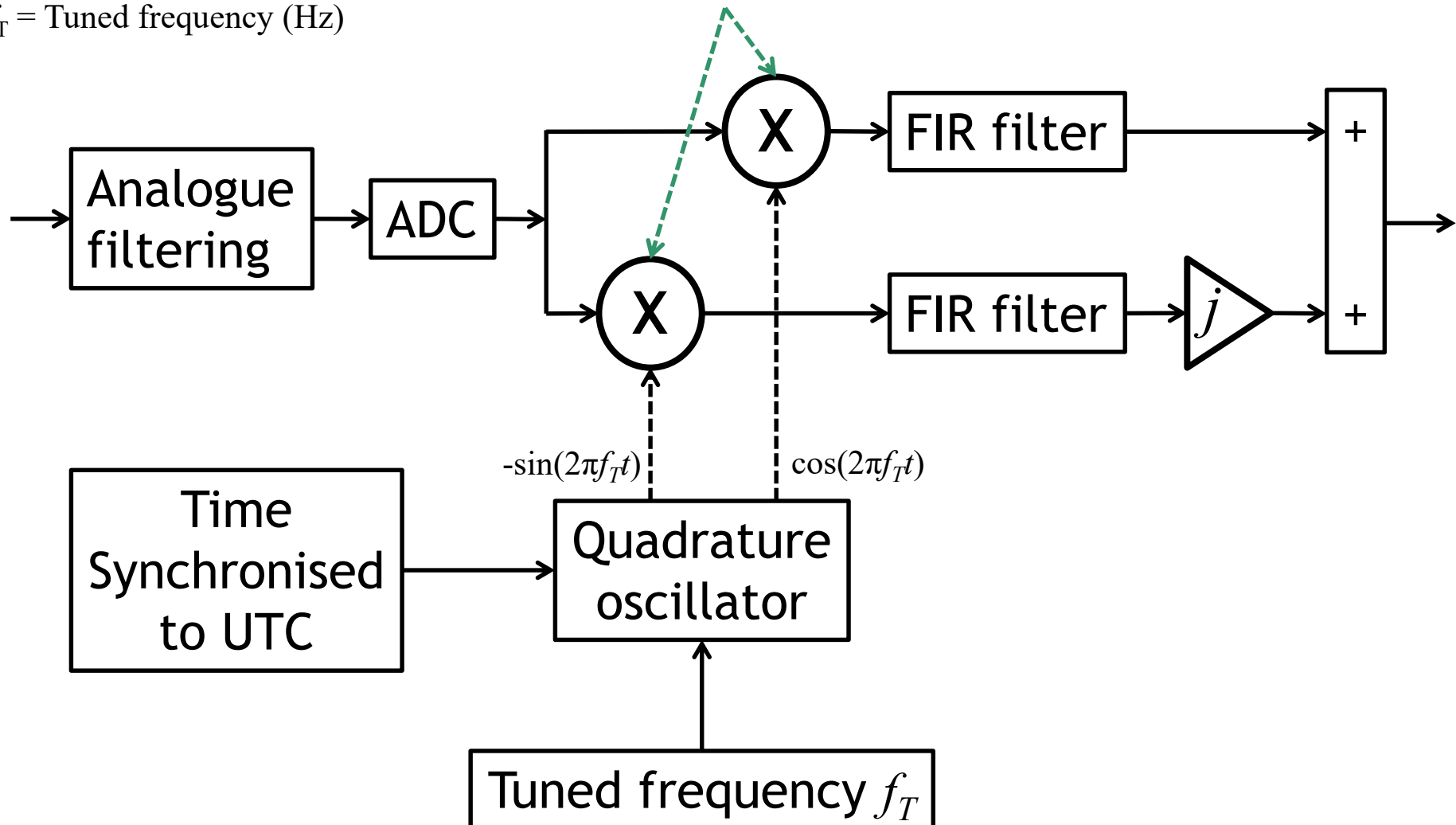
General PMU architecture (single phase section)

Heterodyning

f_0 = Nominal frequency (Hz)

f = Actual fundamental frequency (Hz)

f_T = Tuned frequency (Hz)



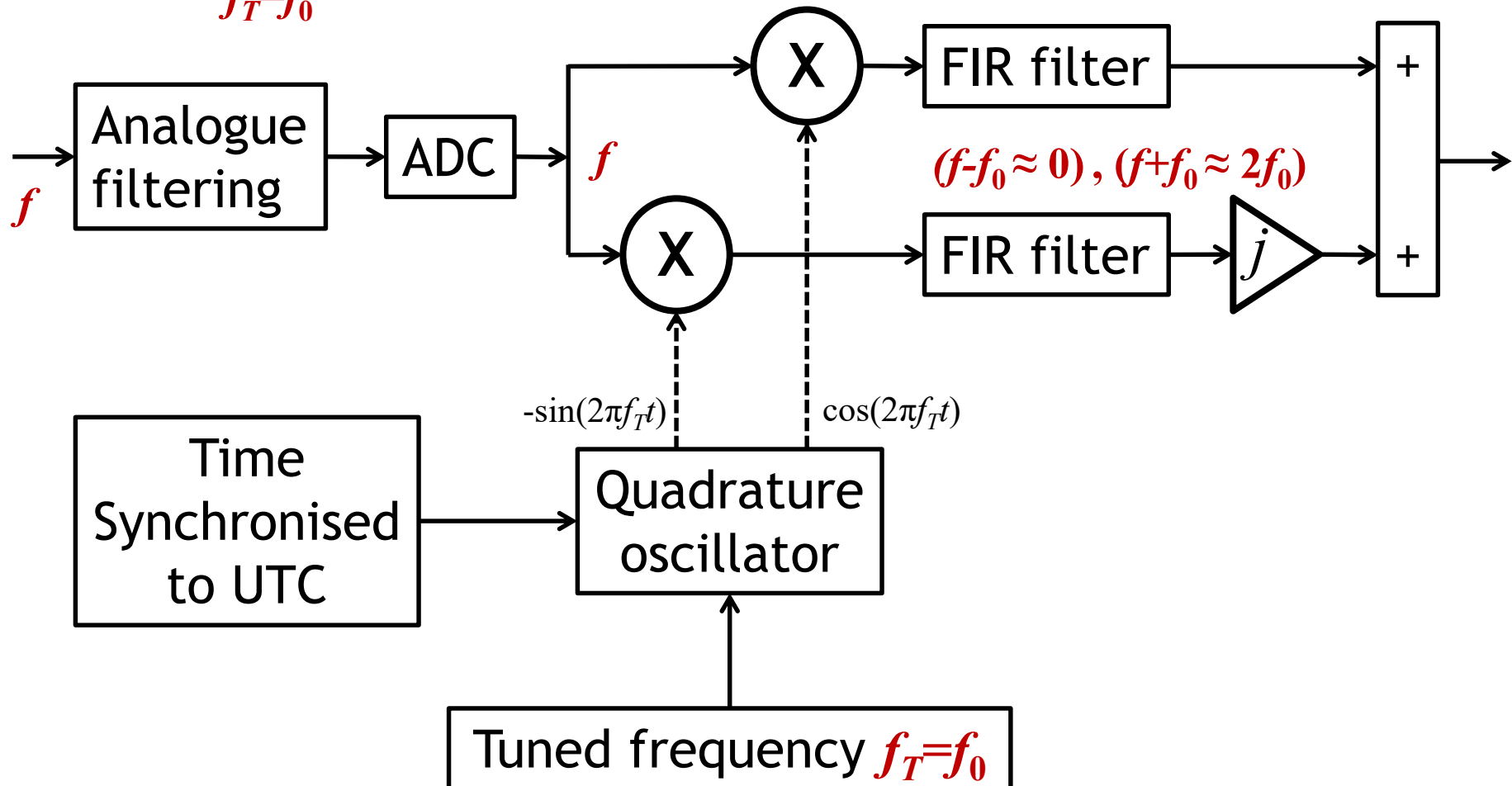
Fixed-filter PMU architecture (single phase section)

f_0 = Nominal frequency (Hz)

f = Actual fundamental frequency (Hz)

f_T = Tuned frequency (Hz)

$$f_T = f_0$$



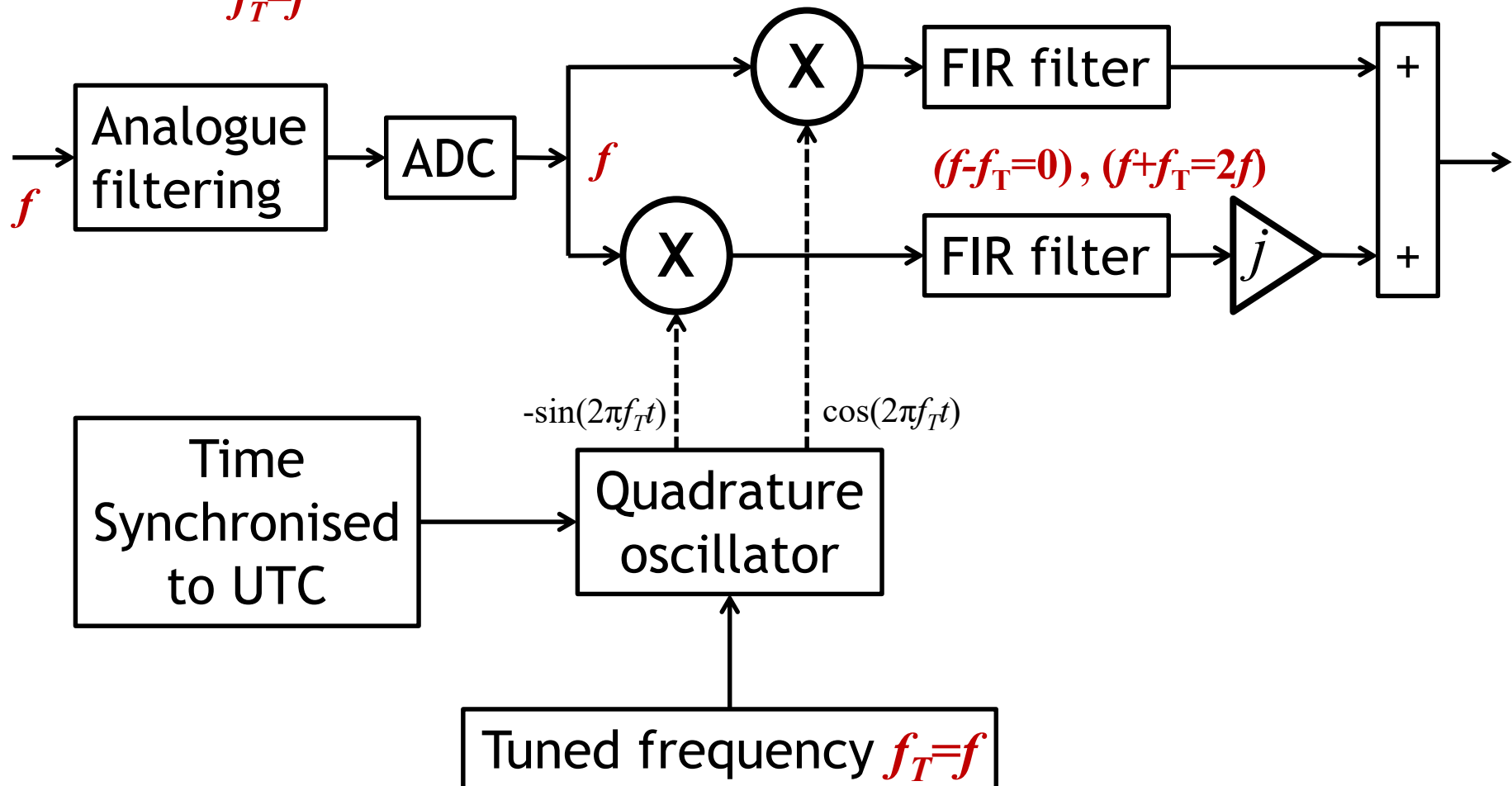
Frequency-tracking PMU architecture (single phase section)

f_0 = Nominal frequency (Hz)

f = Actual fundamental frequency (Hz)

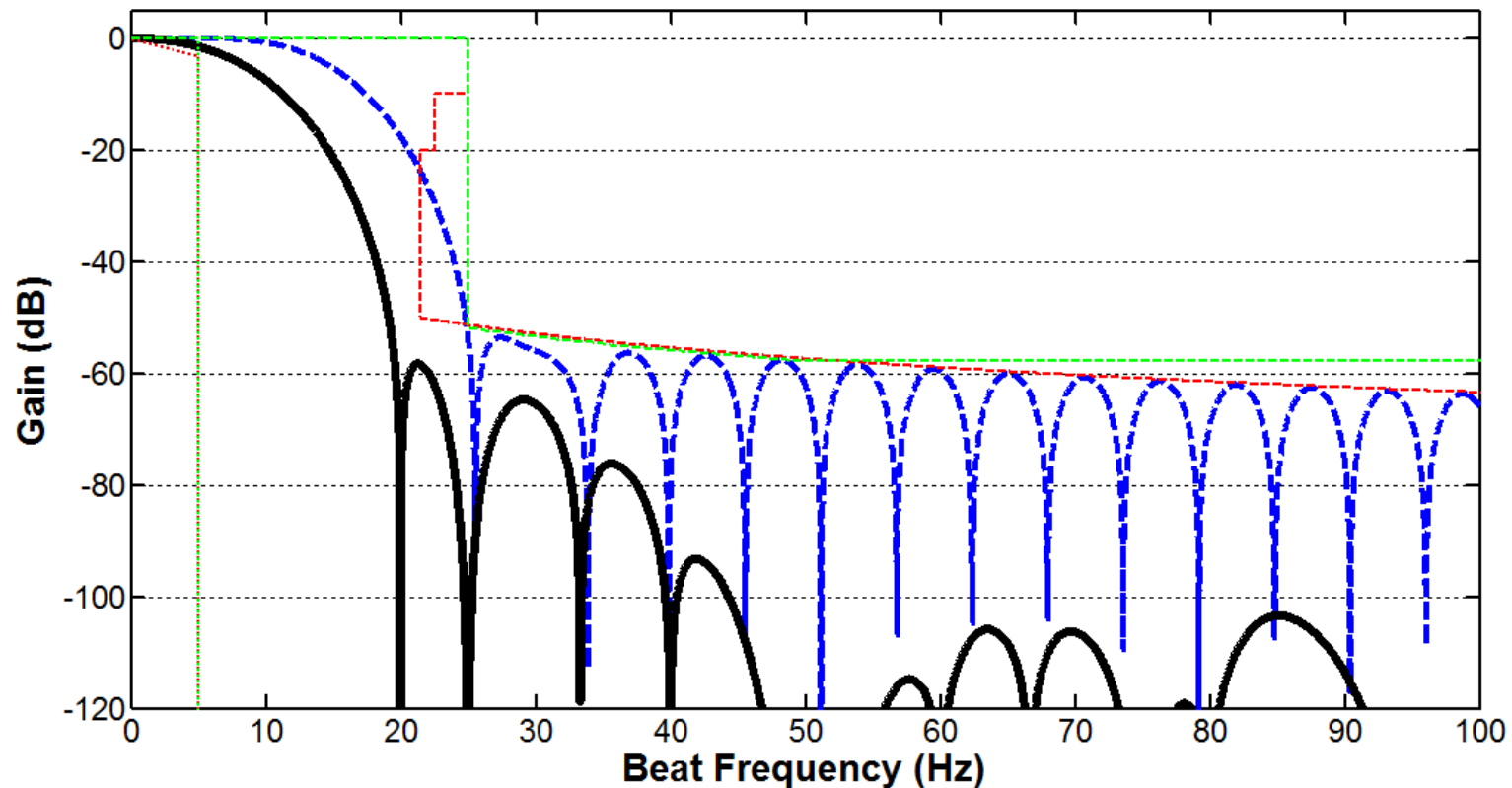
f_T = Tuned frequency (Hz)

$$f_T = f$$



Reference vs. Tracking filter example

$f_0=50$, Reporting rate 50 Hz



- M Reference (C37.118.1a-2014) response
- Filters to meet C37.118.1a amendment : Tracking filter
- Lower (Tracking) mask limit
- Upper (Tracking) mask limit
- Lower (C37) mask limit
- Upper (C37) mask limit

The effect of modulation in the bandwidth test

$$V = \frac{M}{2} e^{j2\pi f_M t} + \frac{M}{2} e^{-j2\pi f_M t}$$

$$V_{Meas} = F(f_M) \frac{M}{2} e^{j2\pi f_M t} + F(-f_M) \frac{M}{2} e^{-j2\pi f_M t}$$

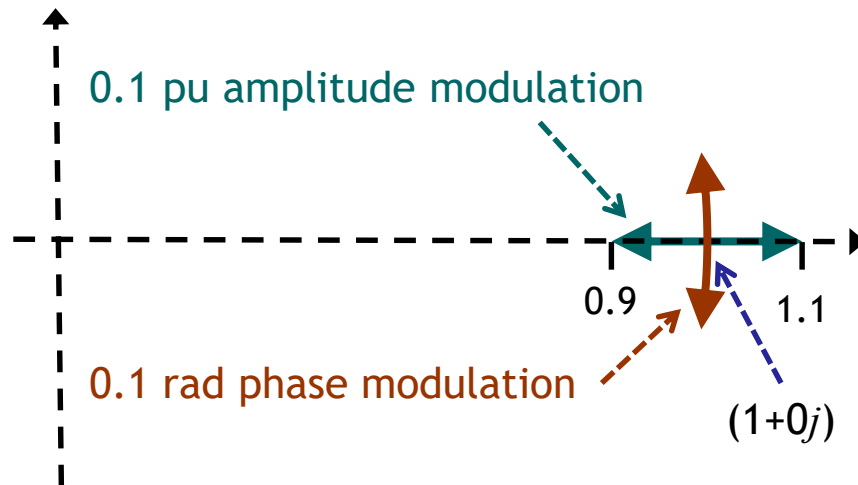
$$TVE = |V_{Meas} - V|$$

$$|F(f_M) - 1| < \frac{TVE_{Limit}}{M}$$

$$|F(f_M)| > 1 - \frac{0.03}{0.1}$$

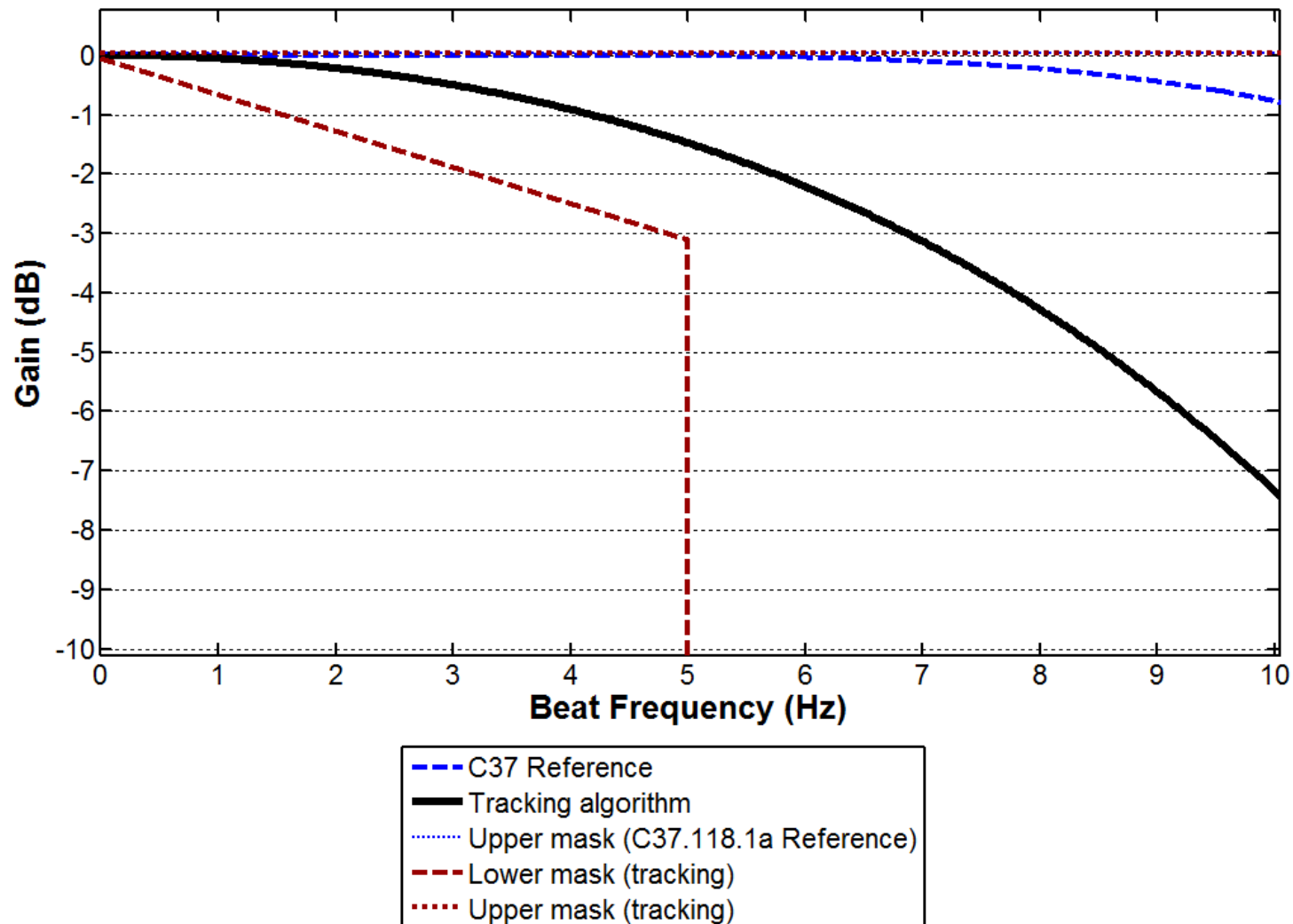
$$|F(f_M)| > 0.7$$

$$F(f_M) > -3.098 \text{ dB}$$

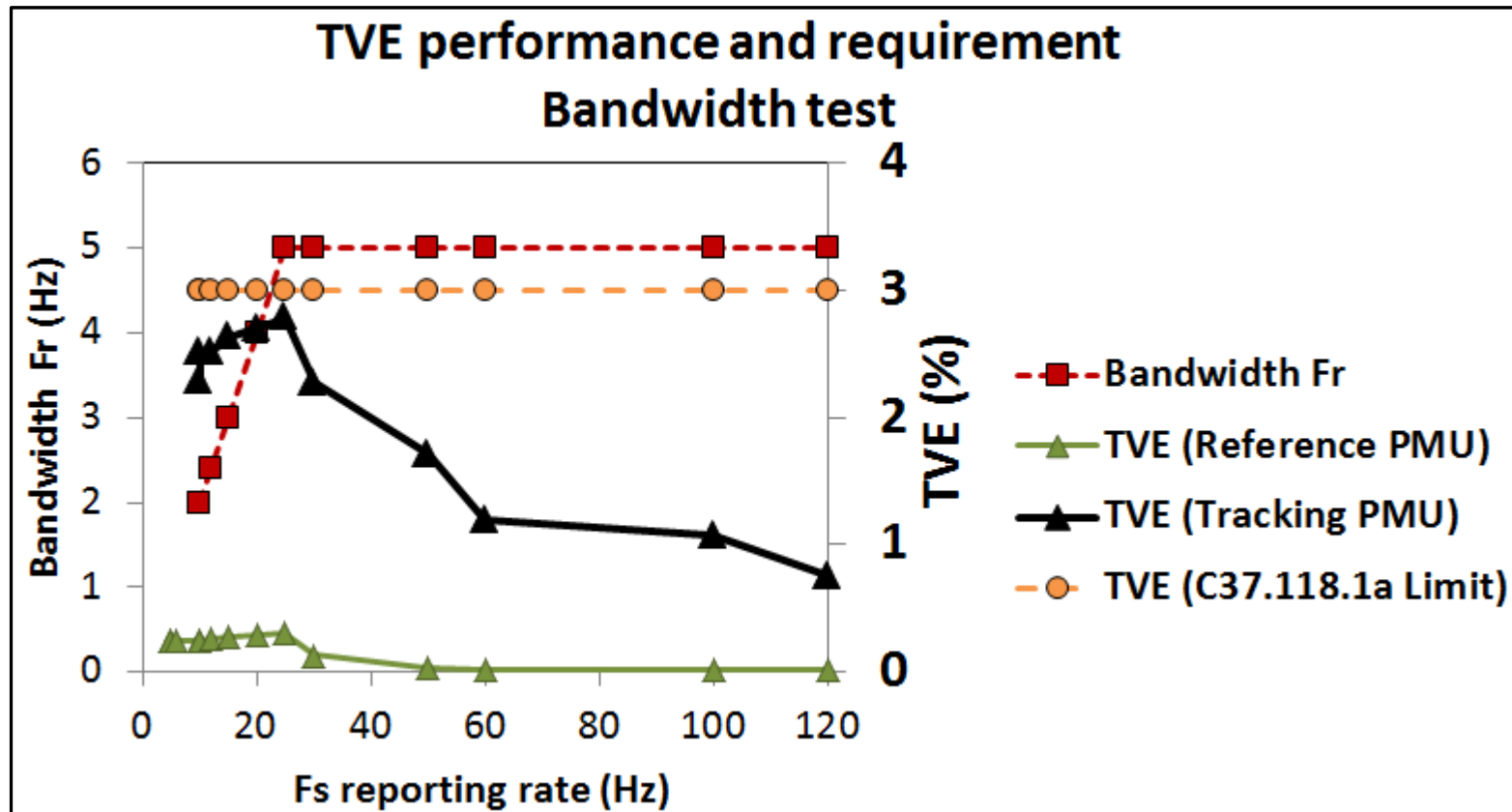


Reference vs. Tracking filter example

$f_0=50$, Reporting rate 50 Hz



Bandwidth test – TVE

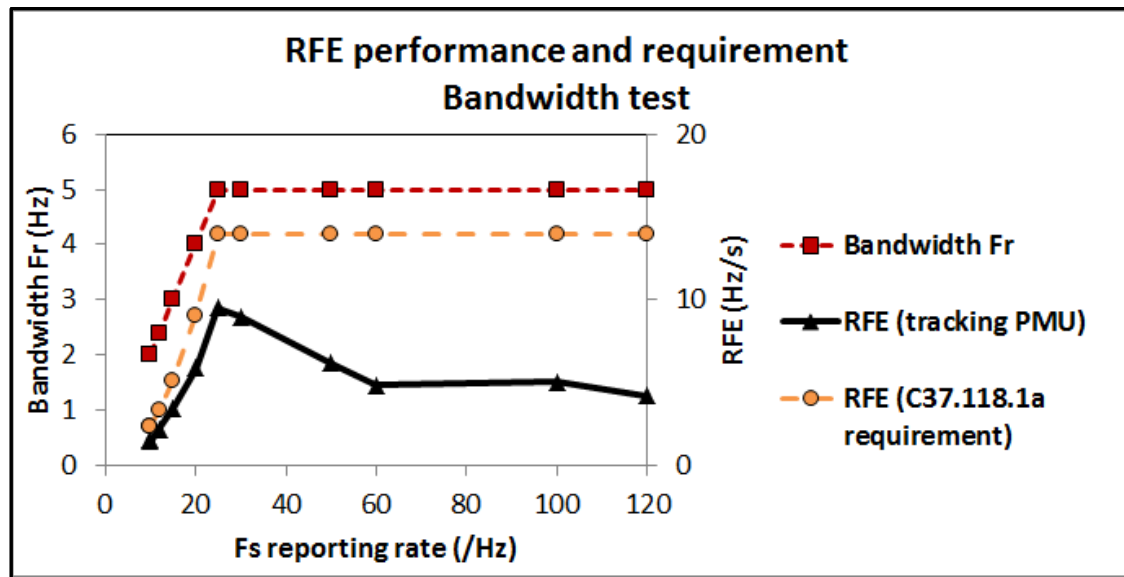
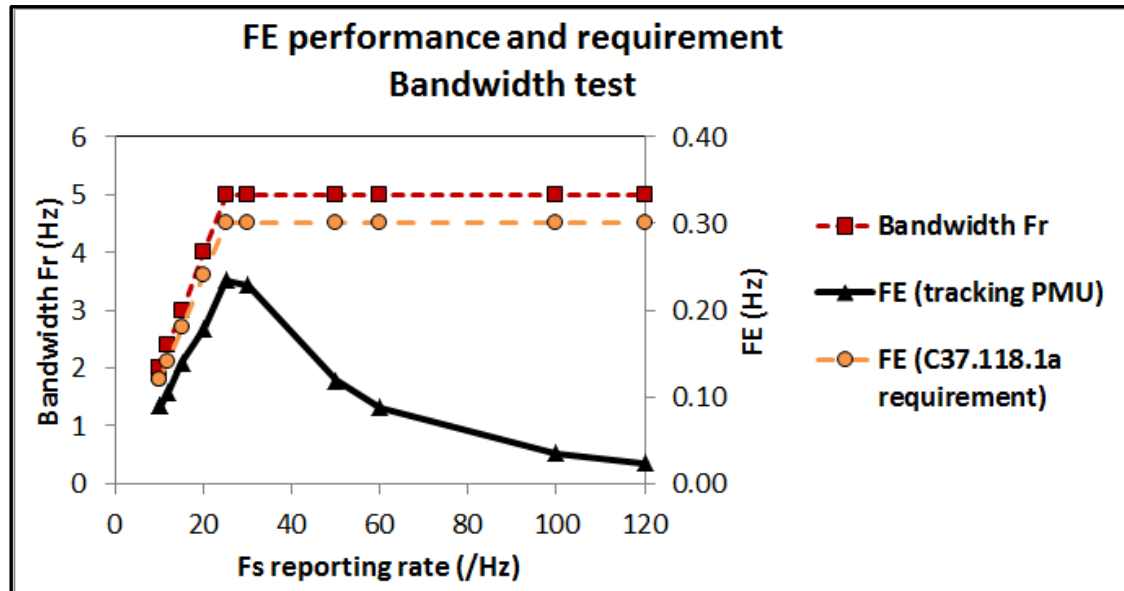


Bandwidth testing

C37.118.1a-2014

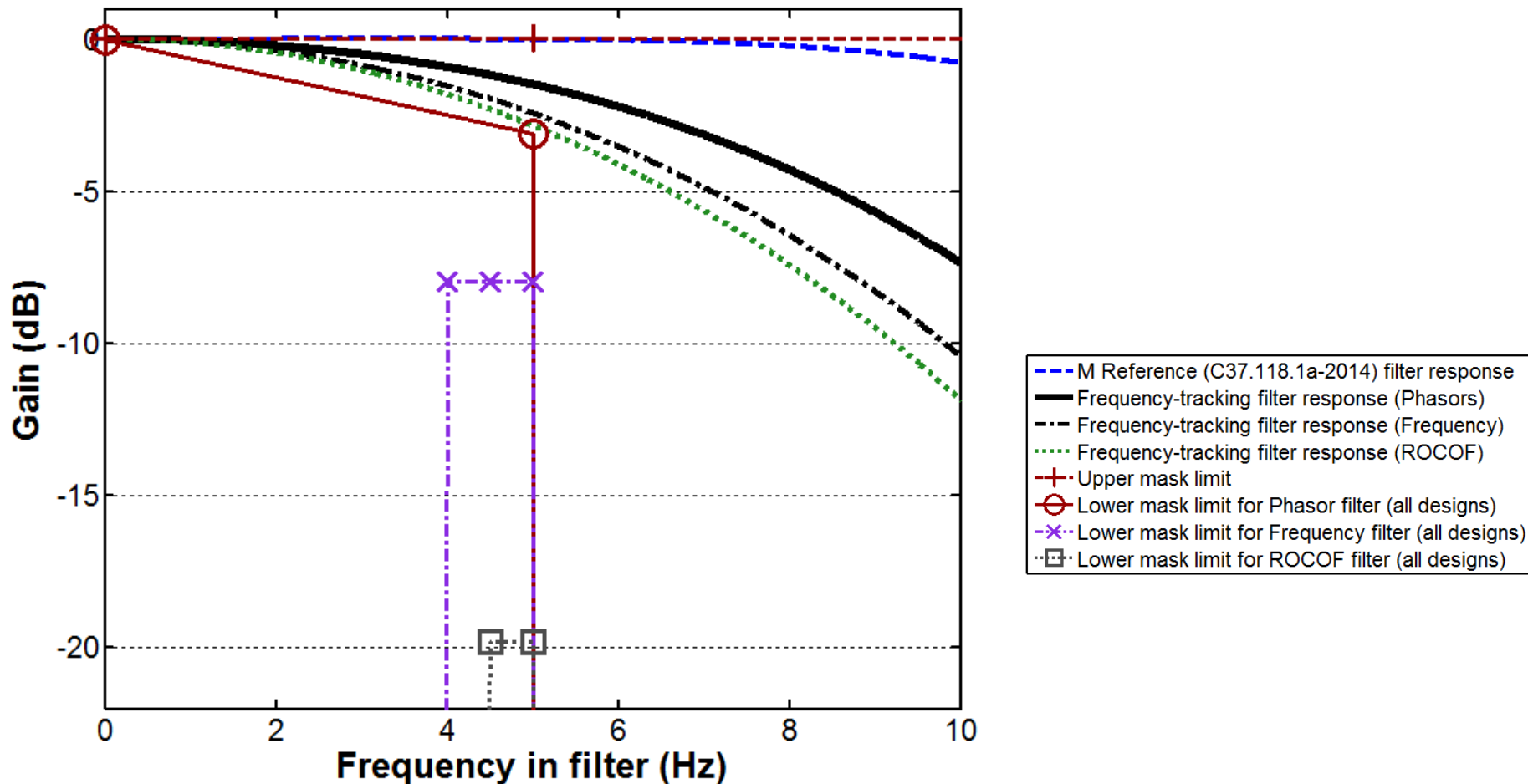
F & ROCOF performance limits	Error requirements for Compliance					
	P Class			M Class		
Reporting Rate F_s (Hz)	F_r (Hz)	Max FE	Max RFE	F_r (Hz)	Max FE	Max RFE
10	1	0.03	0.6	2	0.12	2.3
12	1.2	0.04	0.8	2.4	0.14	3.3
15	1.5	0.05	1.3	3	0.18	5.1
20	2	0.06	2.3	4	0.24	9.0
25	2	0.06	2.3	5	0.30	14
30	2	0.06	2.3	5	0.30	14
50	2	0.06	2.3	5	0.30	14
60	2	0.06	2.3	5	0.30	14
Formulas	$\min(F_s/10, 2)$	$0.03 * F_r$	$0.18 * \pi * F_r^2$	$\min(F_s/5, 5)$	$0.06 * F_r$	$0.18 * \pi * F_r^2$

Bandwidth test – Frequency Error (FE) & ROCOF ERROR (RFE)



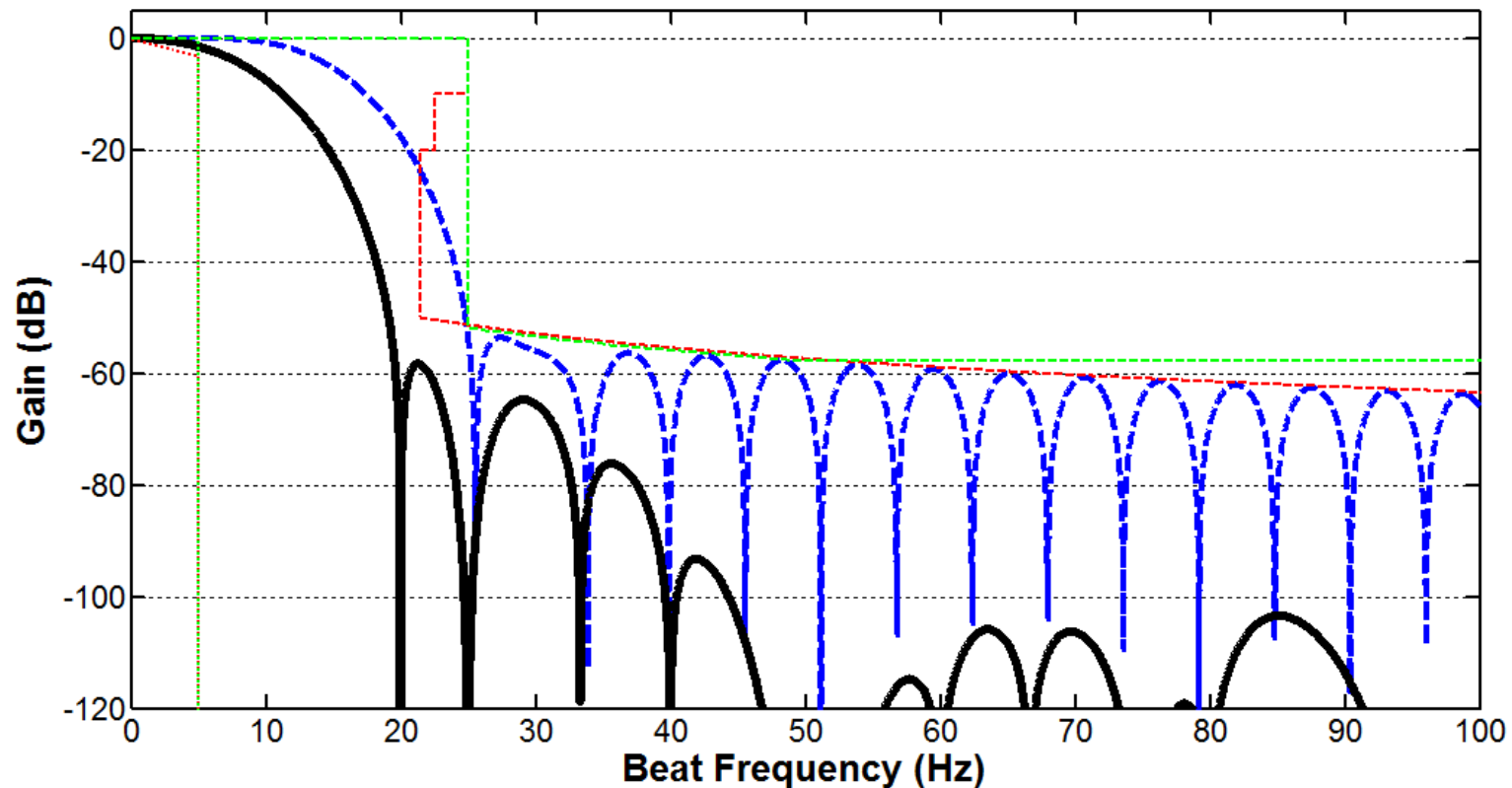
Reference vs. Tracking filter example

$f_0=50$, Reporting rate $F_S=50$ Hz



Reference vs. Tracking filter example

$f_0=50$, Reporting rate 50 Hz



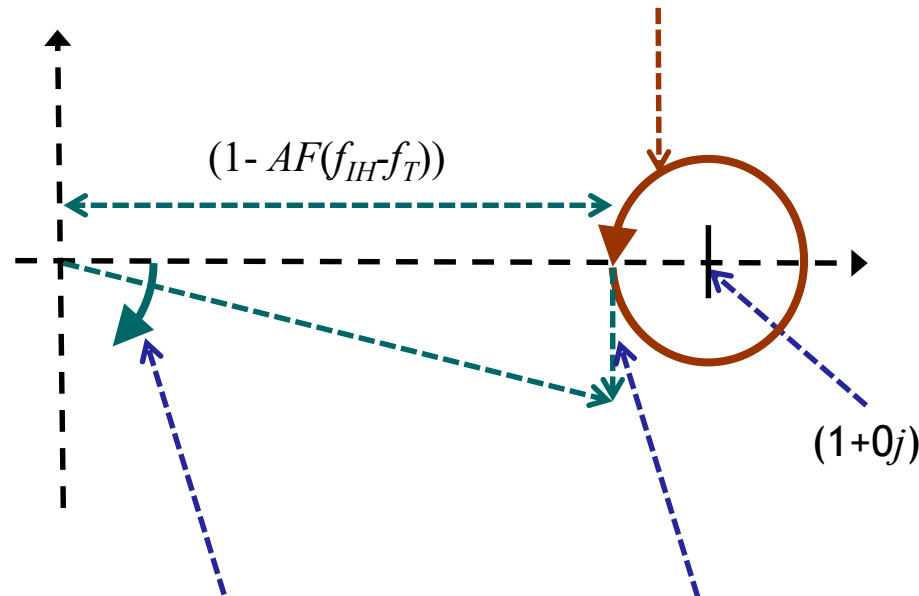
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Frequency error during OOB testing

Interharmonic at $2\pi f_{IH}$

Radius $AF(f_{IH}f_T)$

- where $A=0.1$ pu
- $F(f_{IH}f_T)$ is filter gain at $(f_{IH}f_T)$
- Deviation rotates at $2\pi \cdot (f_{IH}-f)$



Frequency deviation

$$\frac{2\pi \cdot (f_{IH}-f) \cdot AF(f_{IH}-f_T)}{2\pi \cdot (1 - AF(f_{IH}-f_T))}$$

Trajectory speed
at closest approach

$$2\pi \cdot (f_{IH}-f) \cdot AF(f_{IH}-f_T)$$

Determining the required filter Mask for OOB testing

Frequency deviation

$$\frac{2\pi \cdot (f_{IH} - f) \cdot AF(f_{IH} - f_T)}{2\pi \cdot (1 - AF(f_{IH} - f_T))}$$

Frequency deviation

$$\frac{2\pi \cdot (f_{IH} - f) \cdot AF(f_{IH} - f_T)}{2\pi \cdot (1 - AF(f_{IH} - f_T))}$$

$$F(f_{IH} - f_T) < \frac{FE_{max}}{A \cdot (f_{IH} - f)}$$

Minimum separation
of the interharmonic
from the tuned
(heterodyne) frequency.
Sets the width of the mask.

Maximum separation
of the interharmonic
from the
fundamental frequency, when
($f_{IH} - f_T$) is minimum,
sets the gain (attenuation)
Required at the “closest” mask point.

Out-of-Band testing, $f=f_0$

All algorithms

f_0 = Nominal frequency (Hz)

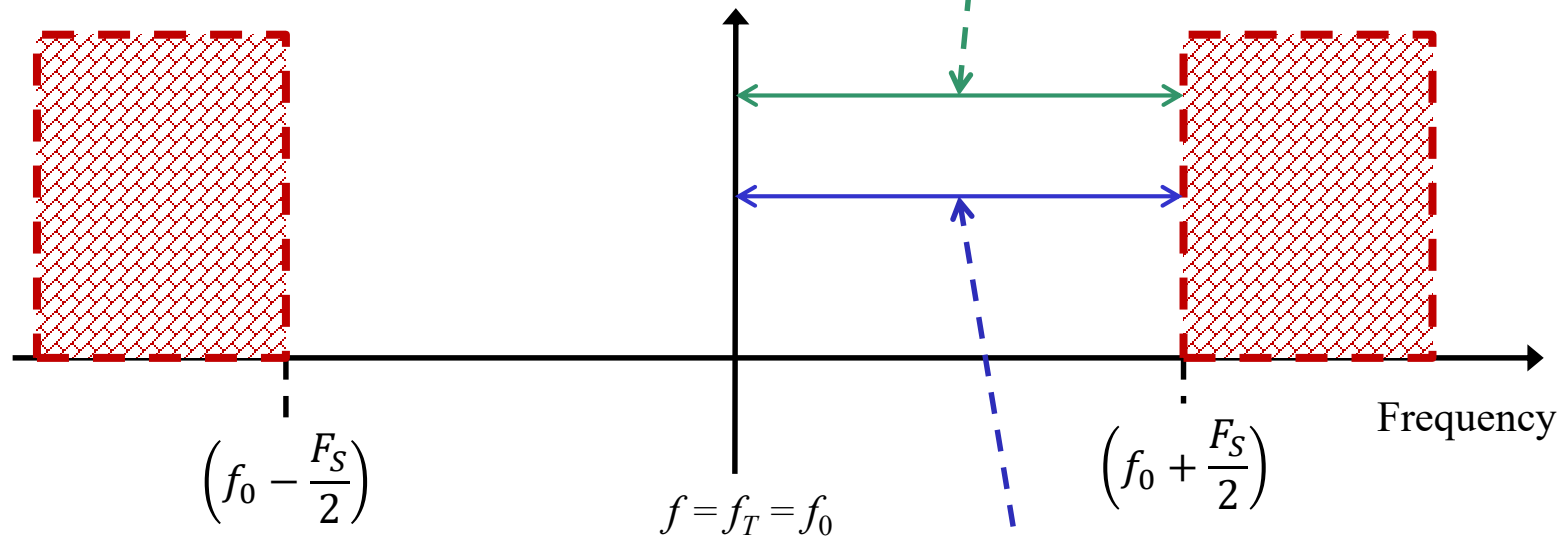
f = Actual fundamental frequency (Hz)

f_T = Tuned frequency (Hz)

Frequency in filter = $(f_{IH} - f_T)$

$$\text{Minimum } f_{IH} \text{ (upper)} = \left(f_0 + \frac{F_S}{2}\right)$$

$$\text{Minimum } (f_{IH} - f_T) = \left(f_0 + \frac{F_S}{2}\right) - f_0 = \left(\frac{F_S}{2}\right)$$



$$\text{Maximum } (f_{IH} - f) = \left(f_0 + \frac{F_S}{2}\right) - f_0 = \left(\frac{F_S}{2}\right)$$

Mask width is “normal” $\left(\frac{F_S}{2}\right)$ and $(f_{IH} - f)$ tracks exactly with $(f_{IH} - f_T)$.

Out-of-Band testing, $f = f_0 - \frac{F_S}{20}$

Fixed-filter algorithm

f_0 = Nominal frequency (Hz)

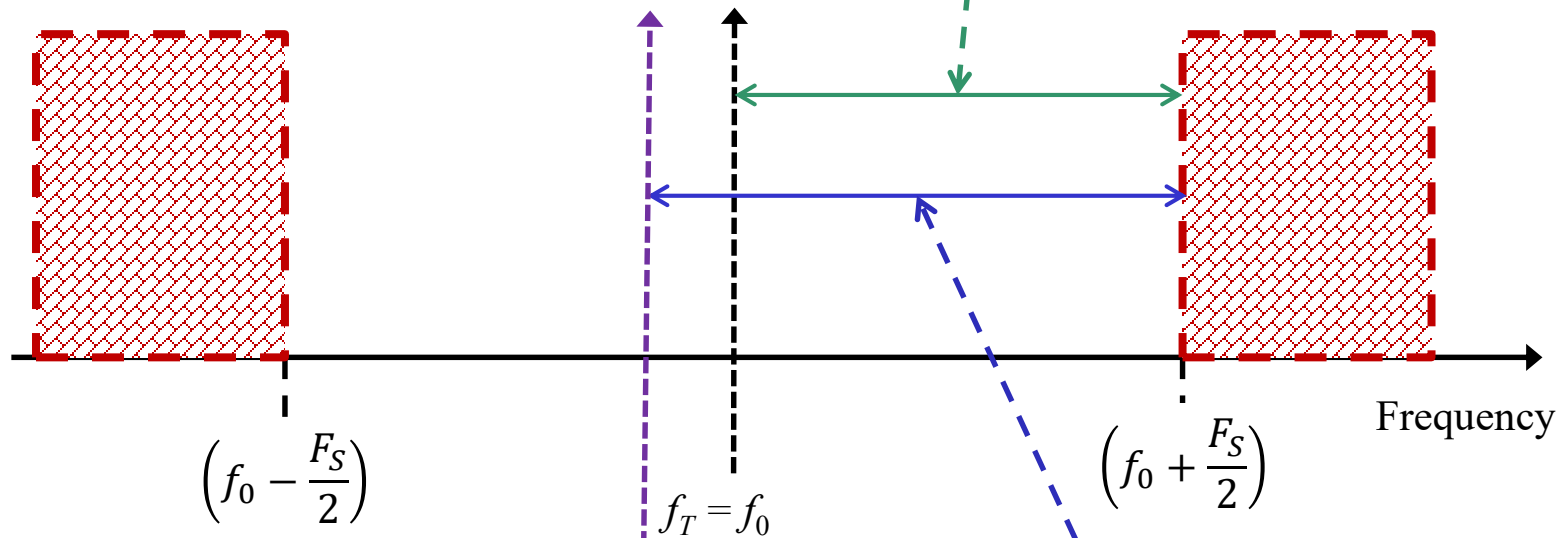
f = Actual fundamental frequency (Hz)

f_T = Tuned frequency (Hz)

Frequency in filter = $(f_{IH} - f_T)$

$$\text{Minimum } f_{IH} \text{ (upper)} = \left(f_0 + \frac{F_S}{2}\right)$$

$$\text{Minimum } (f_{IH} - f_T) = \left(f_0 + \frac{F_S}{2}\right) - f_0 = \left(\frac{F_S}{2}\right)$$



$$f = f_0 - \frac{F_S}{20} \quad \text{Maximum } (f_{IH} - f) = \left(f_0 + \frac{F_S}{2}\right) - \left(f_0 - \frac{F_S}{20}\right) = \left(1.1 \frac{F_S}{2}\right)$$

Mask width is “normal” $\left(\frac{F_S}{2}\right)$ but gain needs to be reduced by $20 \cdot \log\left(\frac{1}{1.1}\right) = 0.83$ dB, at the closest frequency, from what you might expect.

Out-of-Band testing, $f = f_0 + \frac{F_S}{20}$

Frequency-tracking algorithm

f_0 = Nominal frequency (Hz)

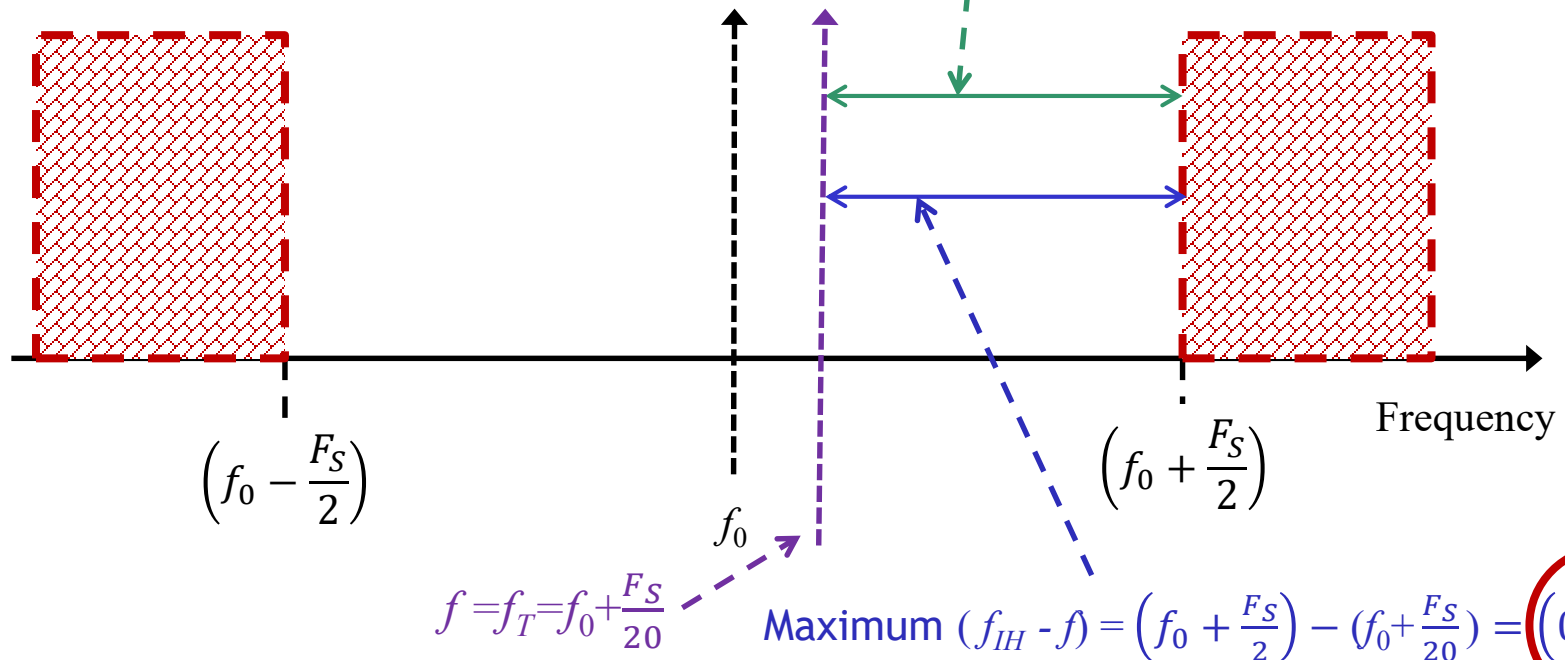
f = Actual fundamental frequency (Hz)

f_T = Tuned frequency (Hz)

Frequency in filter = $(f_{IH} - f_T)$

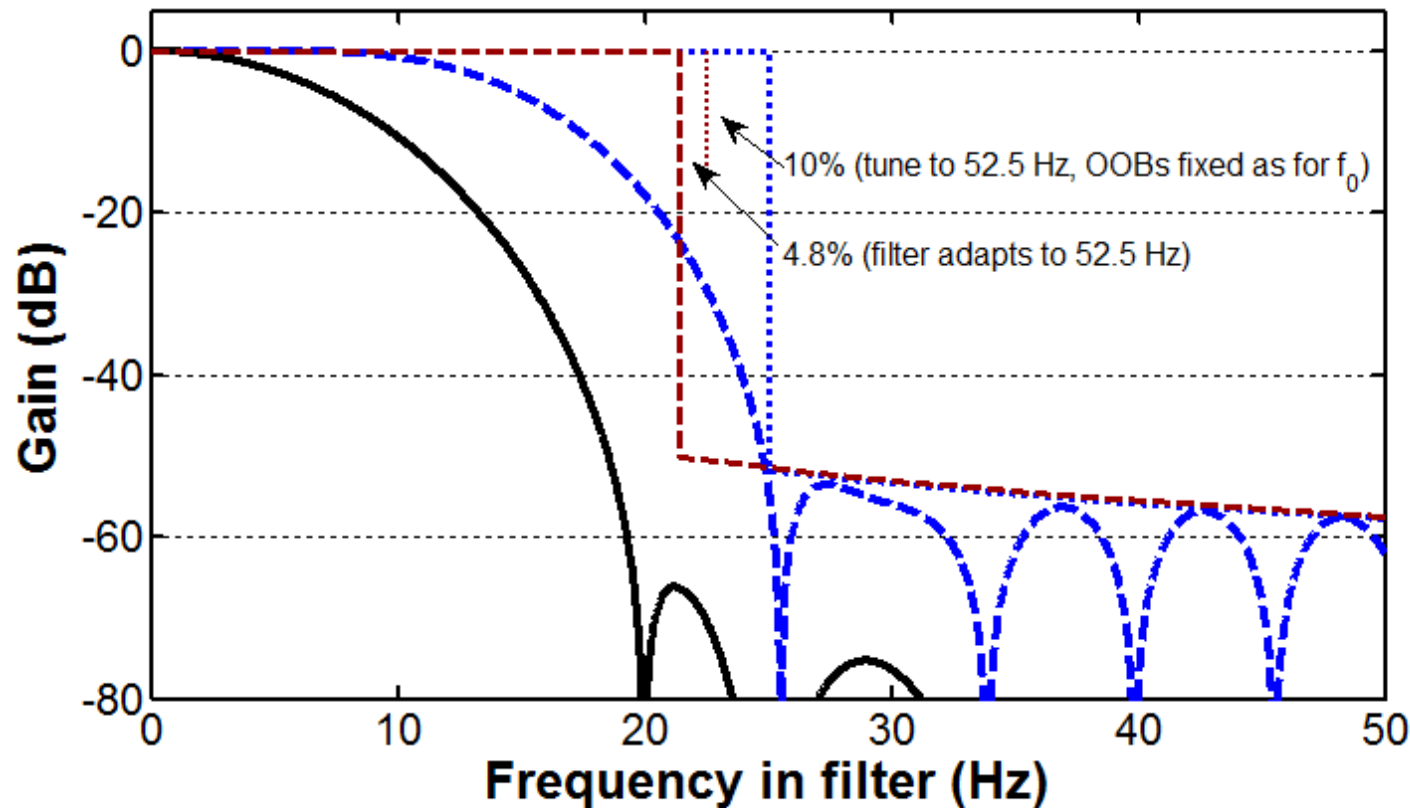
$$\text{Minimum } f_{IH} \text{ (upper)} = \left(f_0 + \frac{F_S}{2}\right)$$

$$\text{Minimum } (f_{IH} - f_T) = \left(f_0 + \frac{F_S}{2}\right) - \left(f_0 + \frac{F_S}{20}\right) = 0.9 \left(\frac{F_S}{2}\right)$$



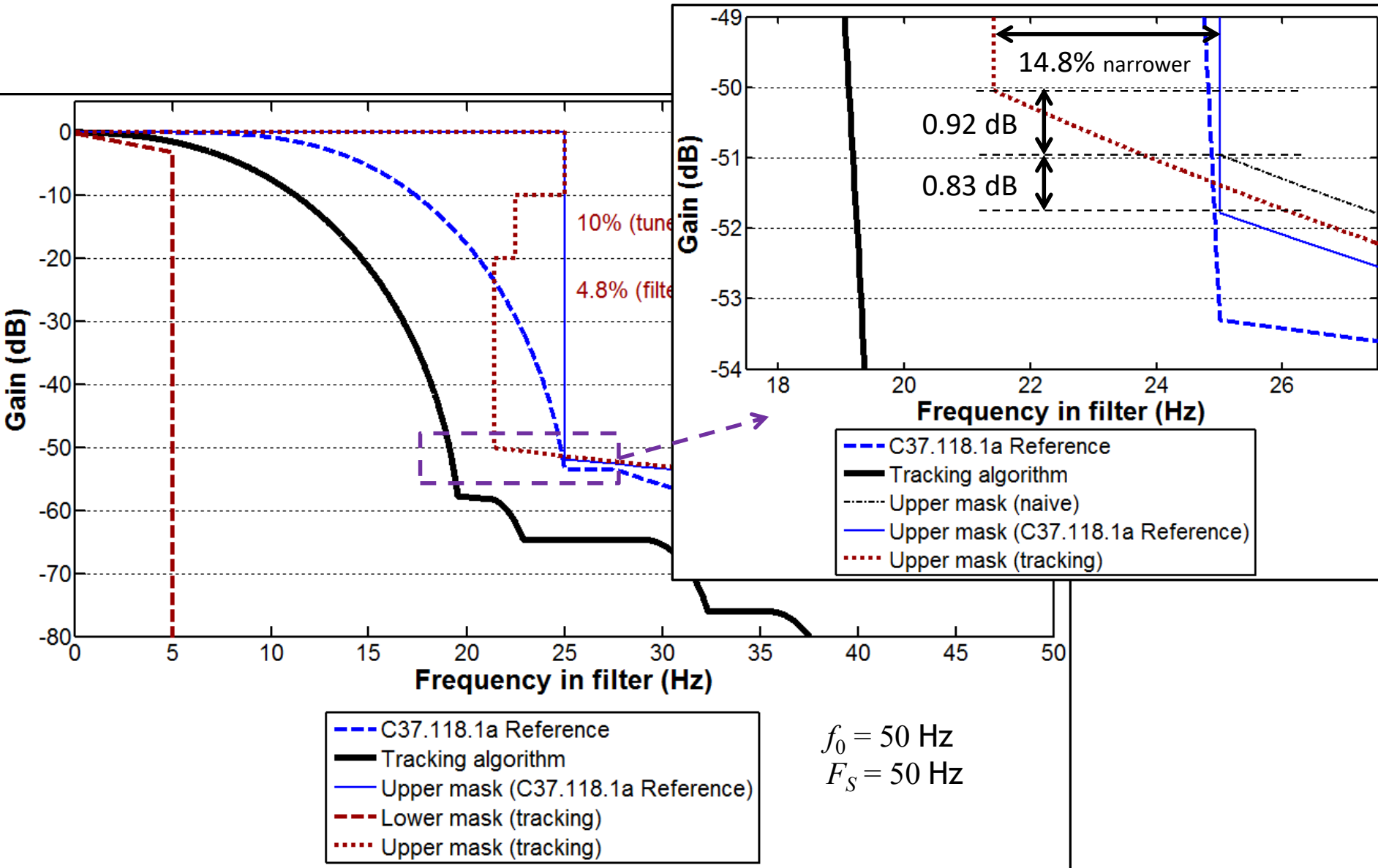
Mask frequency width is reduced by 10% from $\left(\frac{F_S}{2}\right)$ but gain can be $20 \cdot \log \left(\frac{1}{0.9}\right) = 0.92$ dB higher, at the closest frequency, from what you might expect.

Simplified OOB requirements and examples, $f_0=50$ Hz, $F_S=50$ Hz

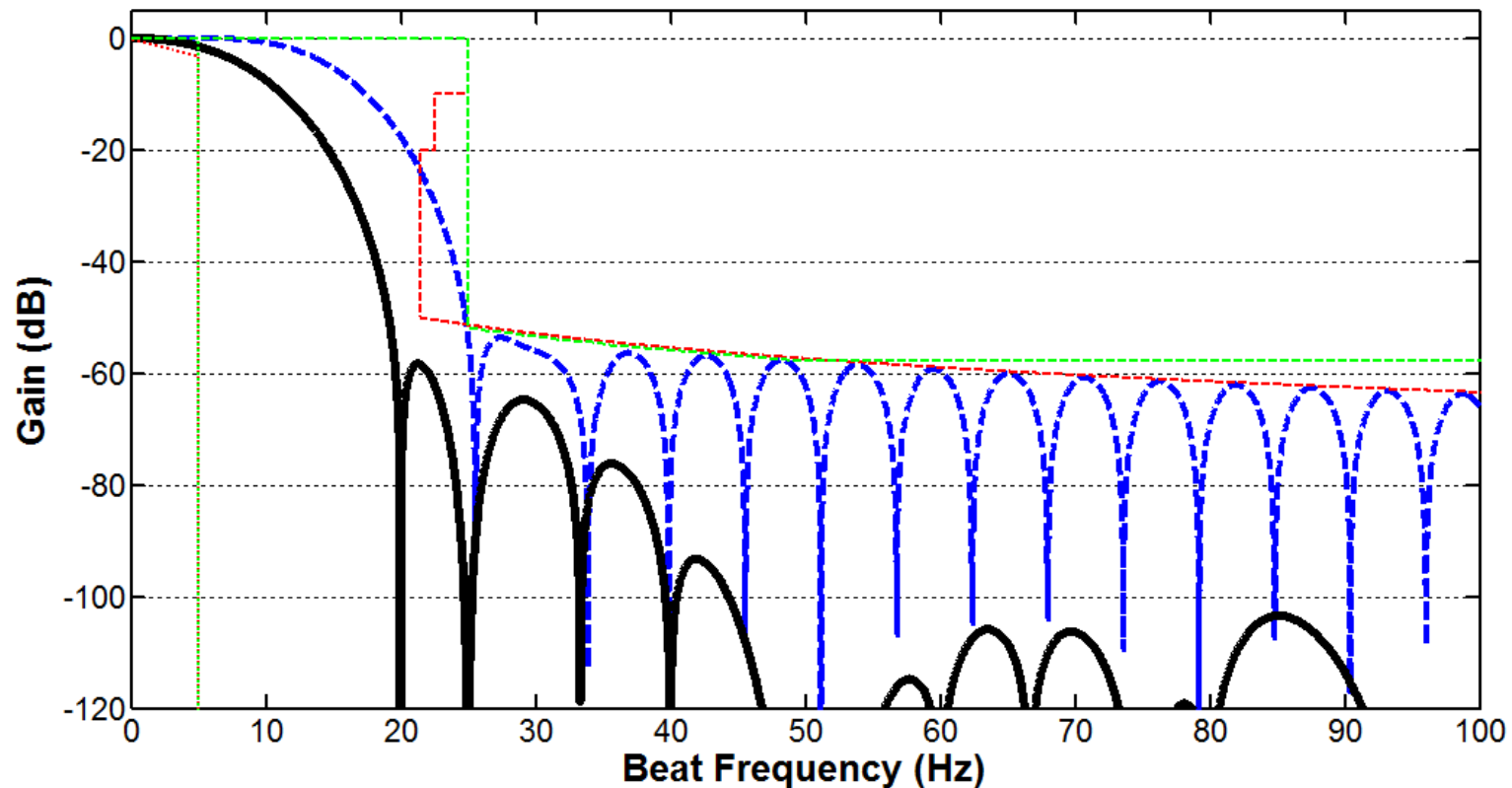


- M Reference (C37.118.1a-2014) filter response
- Frequency-tracking filter response (Frequency)
- Upper mask limit for Frequency filter (Fixed-filter designs)
- - - Upper mask limit for Frequency filter (Frequency-tracking designs)
- Indication of 10% filter mask reduction (Frequency-tracking designs)

Simplified OOB requirements and examples, $f_0=50$ Hz, $F_S=50$ Hz



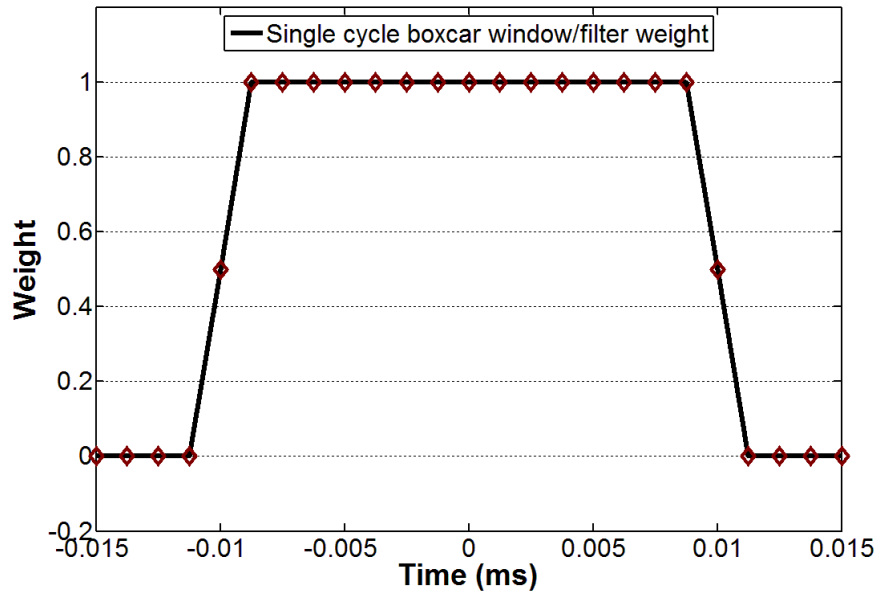
Cascaded boxcar filters, $f_0=50$ Hz, $F_S=50$ Hz



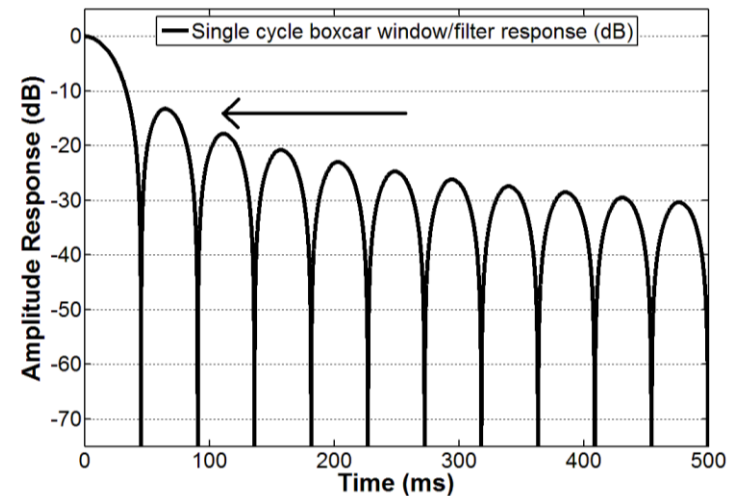
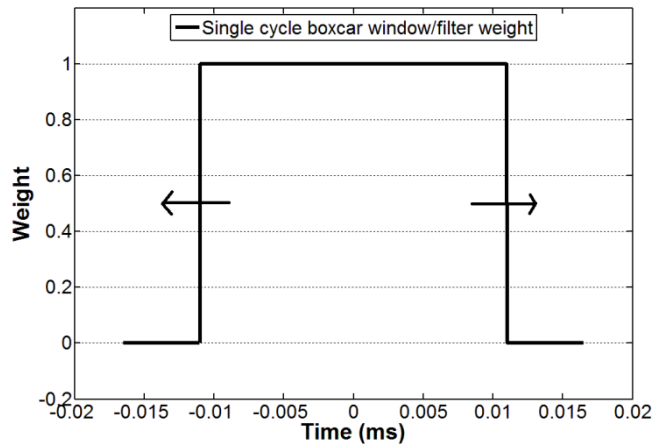
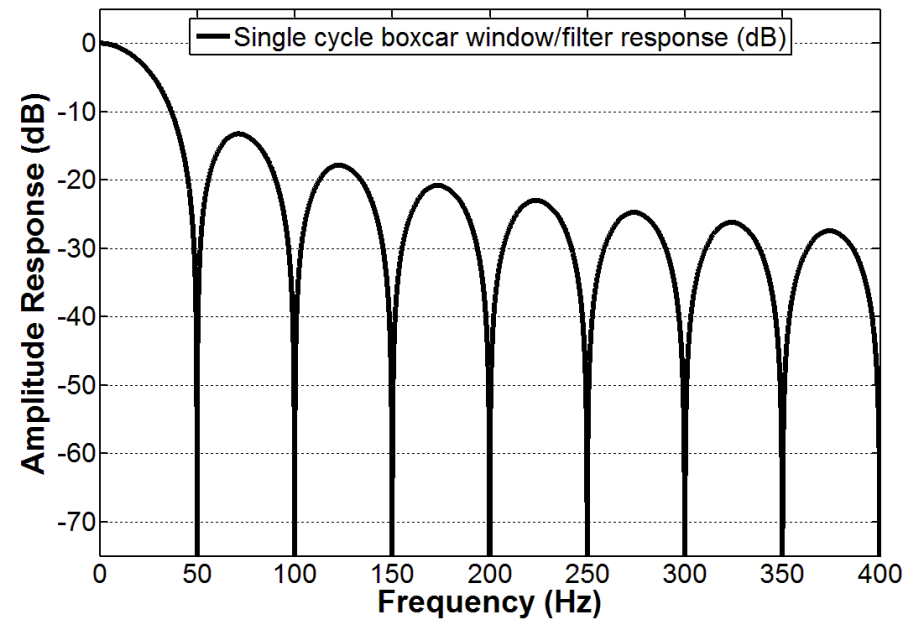
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Boxcar filter properties

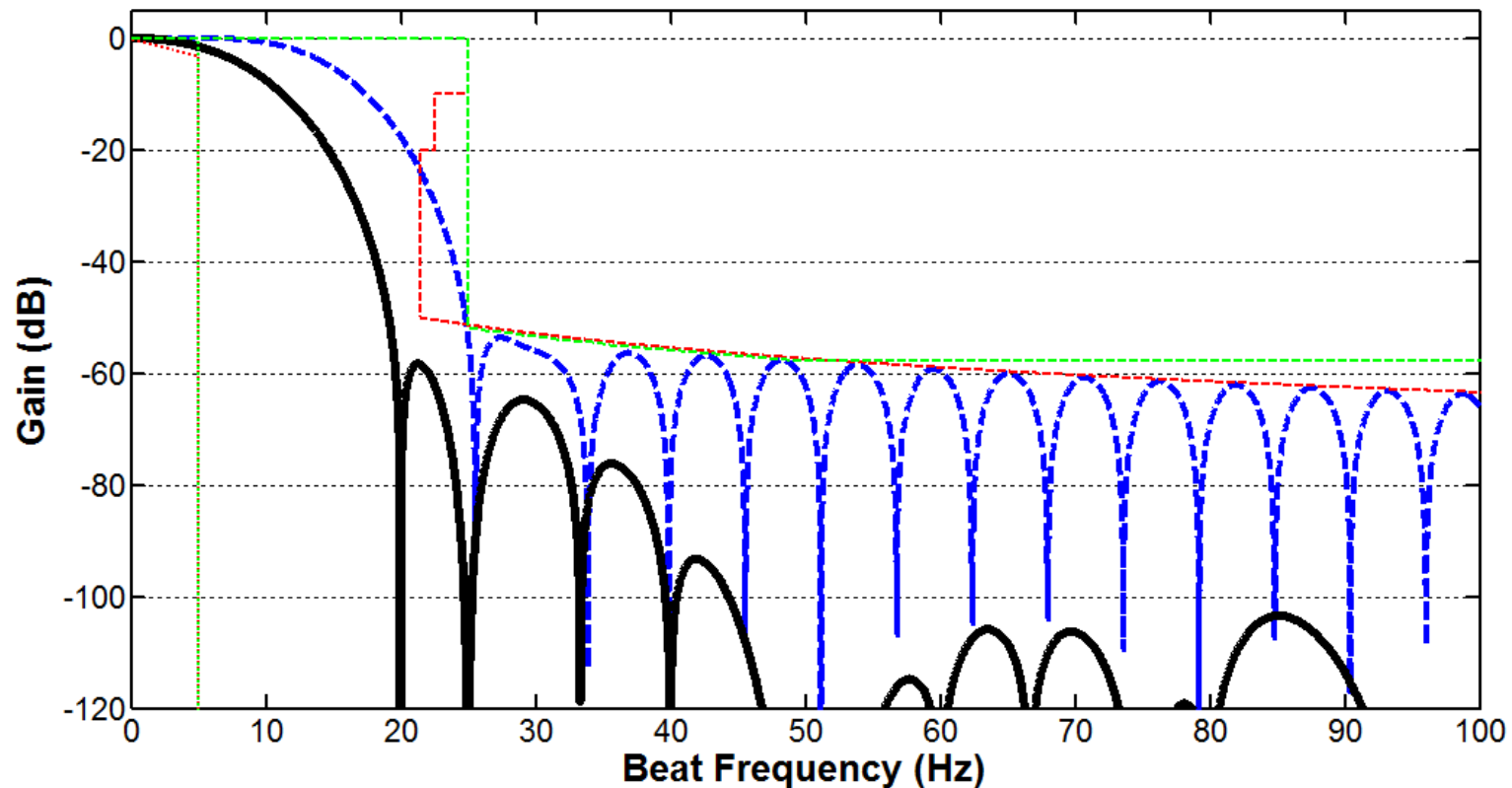
Single cycle boxcar window/filter : $F_{adc} = 0.8\text{kHz}$, $f_0 = 50\text{Hz}$



Single cycle boxcar window/filter response : $F_{adc} = 50\text{kHz}$, $f_0 = 50\text{Hz}$

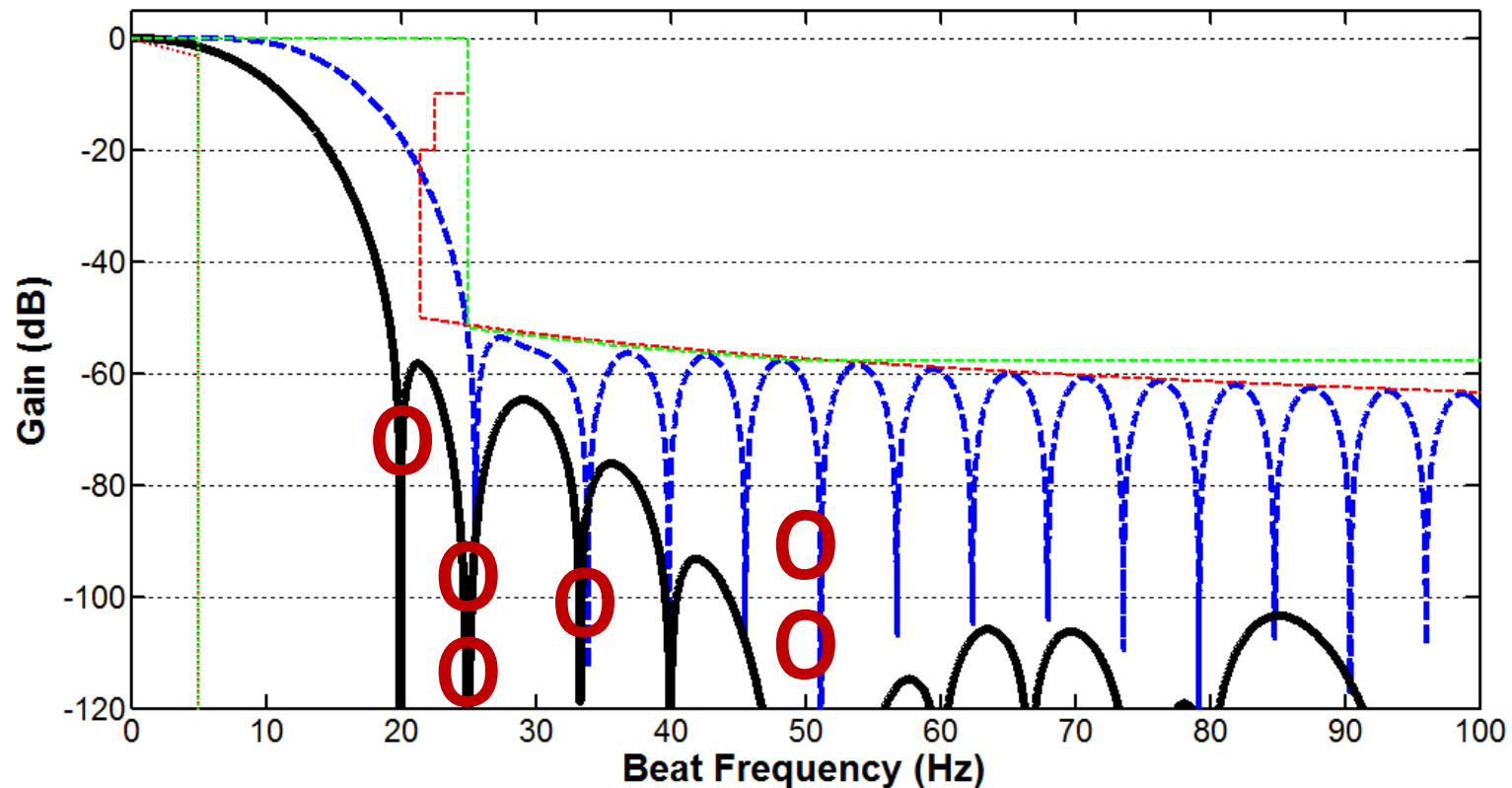


Cascaded boxcar filters example, $f_0=50$ Hz, $F_S=50$ Hz

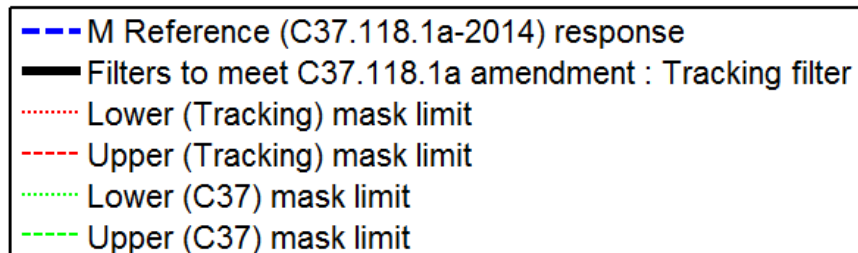


- M Reference (C37.118.1a-2014) response
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- ... Lower (Tracking) mask limit
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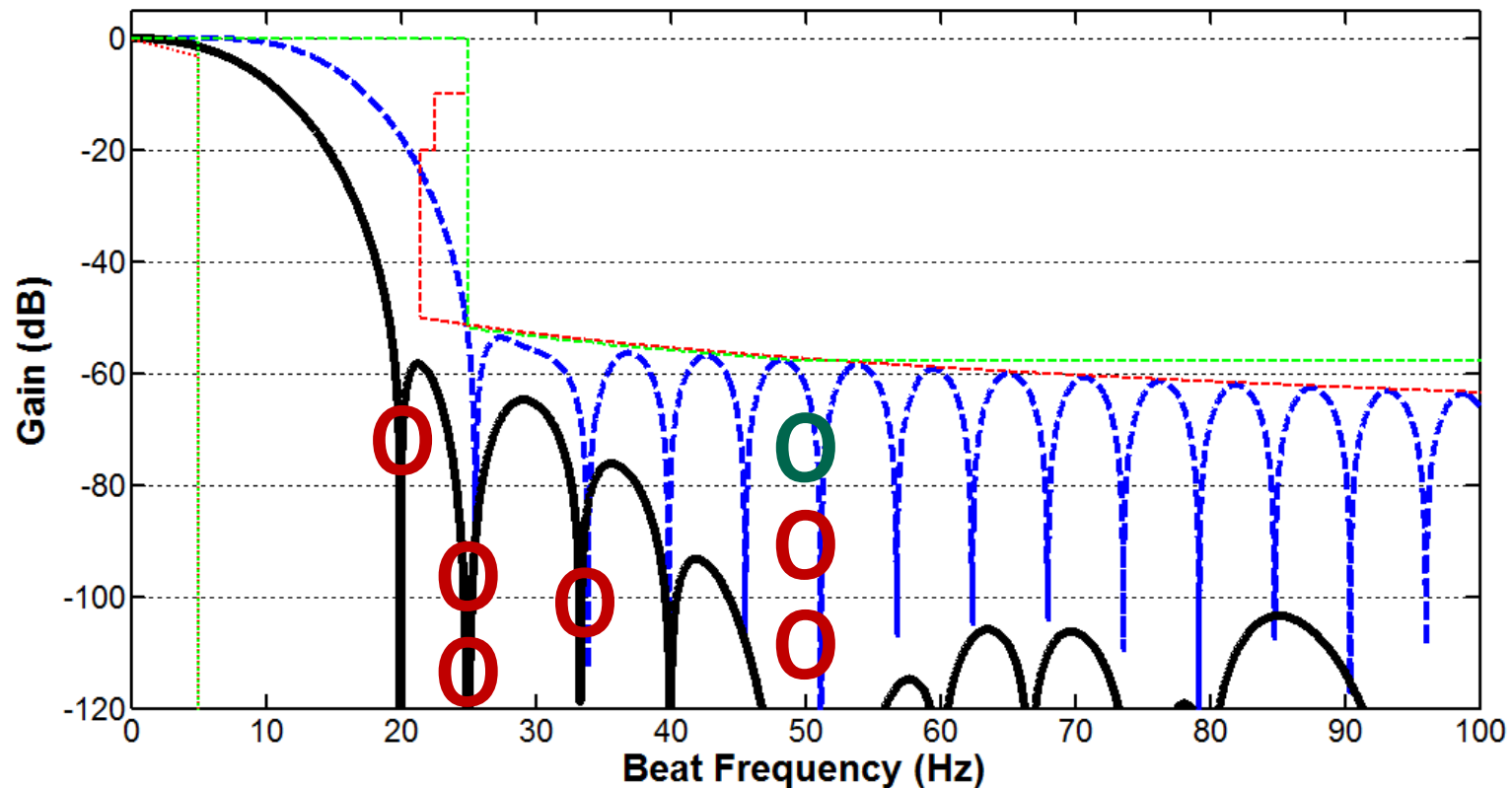
Cascaded boxcar filters example, $f_0=50$ Hz, $F_S=50$ Hz



○ Primary filter zeros

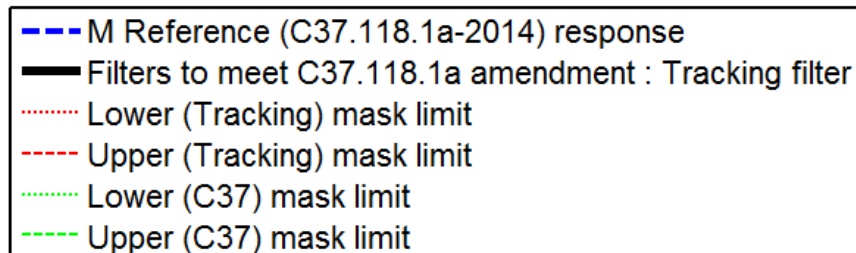


Cascaded boxcar filters example, $f_0=50$ Hz, $F_S=50$ Hz

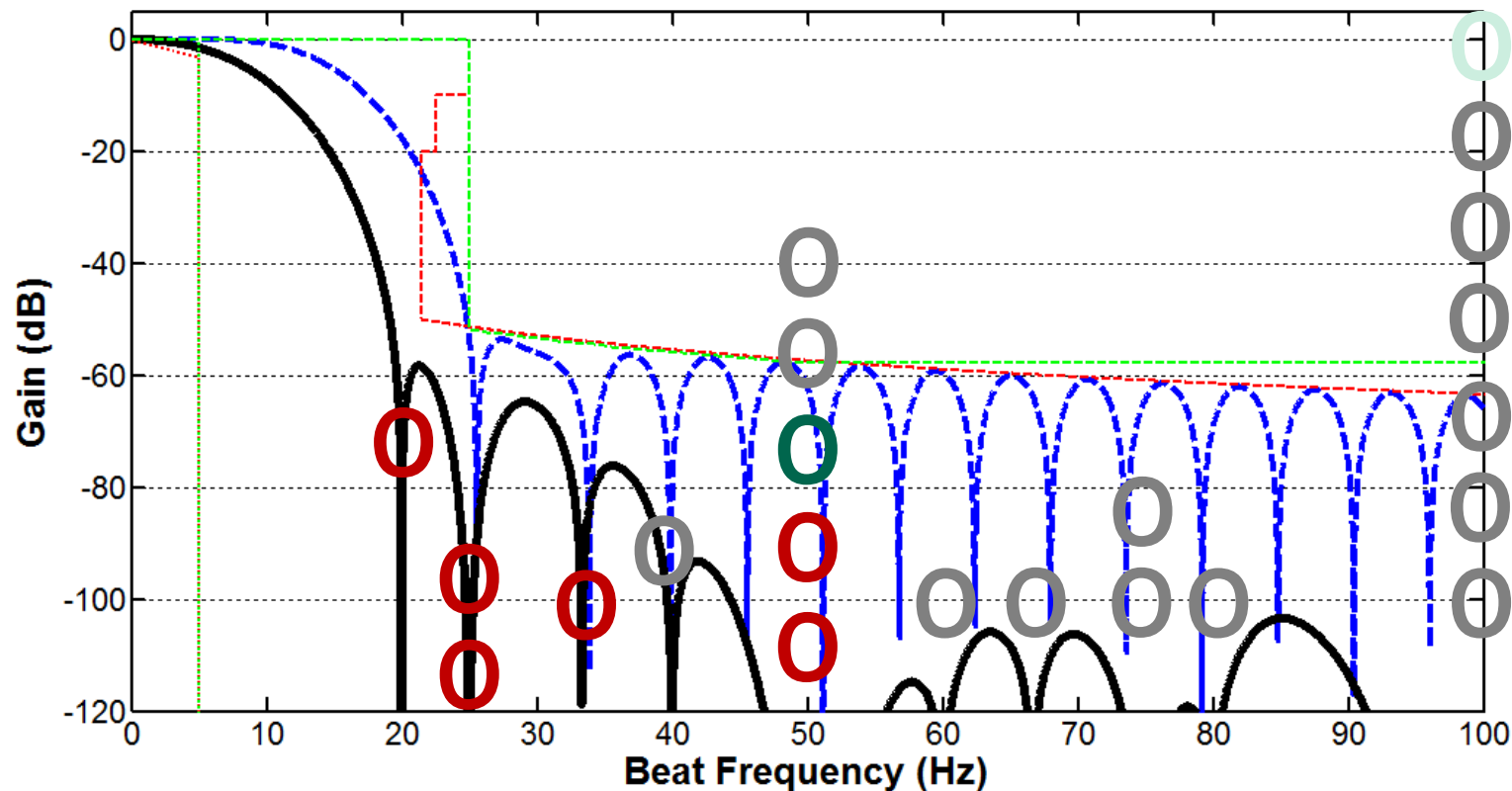


 Primary filter zeros

 Frequency filter
Additional zeros

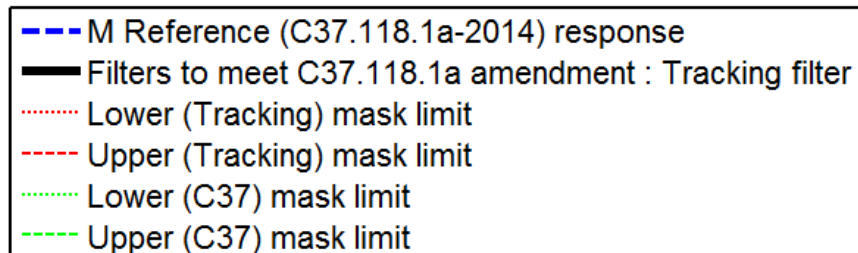


Cascaded boxcar filters example, $f_0=50$ Hz, $F_S=50$ Hz



○ Primary filter zeros

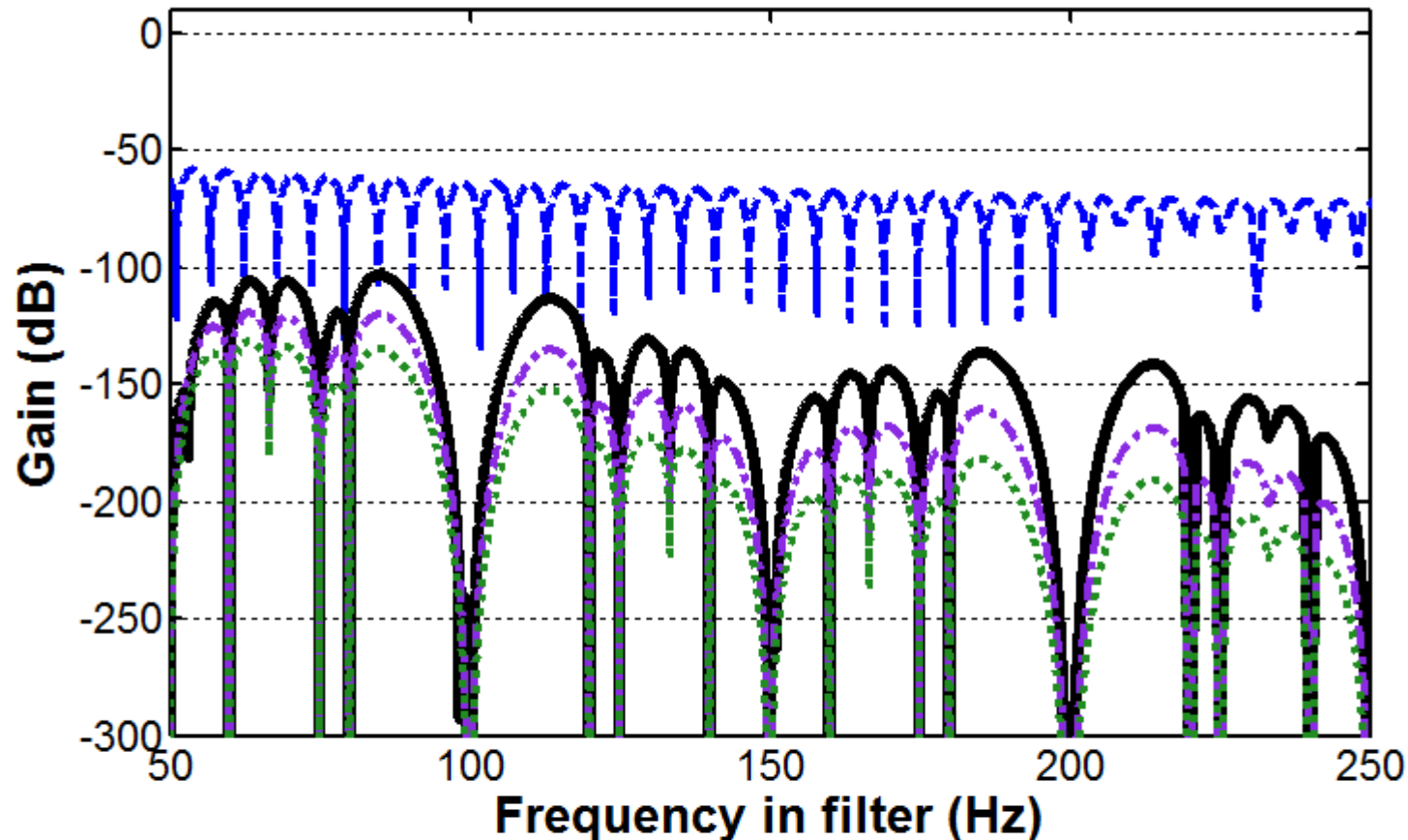
○ Frequency filter
Additional zeros



○ “Harmonic” zeros

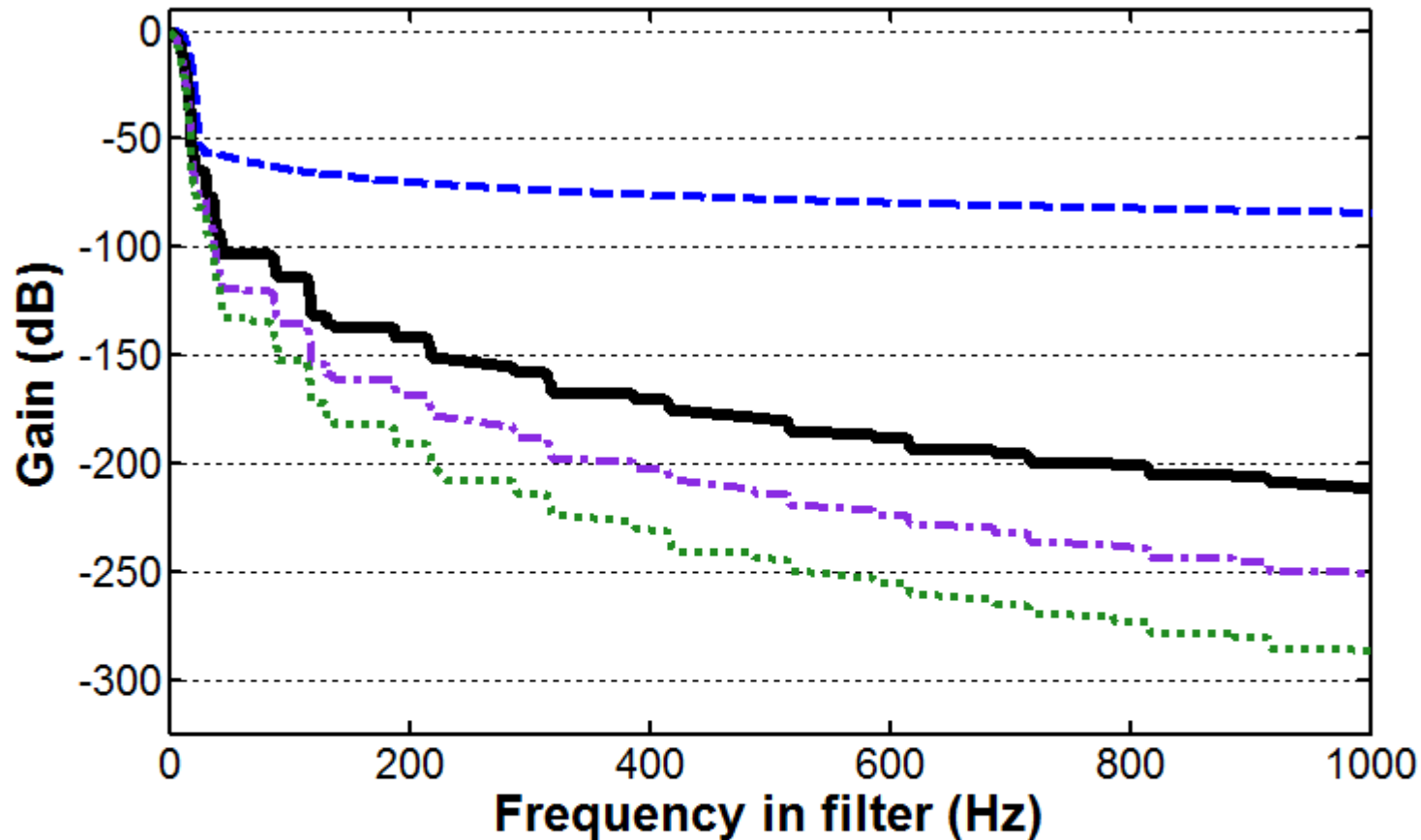
○ Frequency filter
“harmonic” zeros

Cascaded boxcar filters example, $f_0=50$ Hz, $F_S=50$ Hz



- M Reference (C37.118.1a-2014) filter response
- Frequency-tracking filter response (Phasors)
- Frequency-tracking filter response (Frequency)
- Frequency-tracking filter response (ROCOF)

Cascaded boxcar filters example, $f_0=50$ Hz, $F_S=50$ Hz



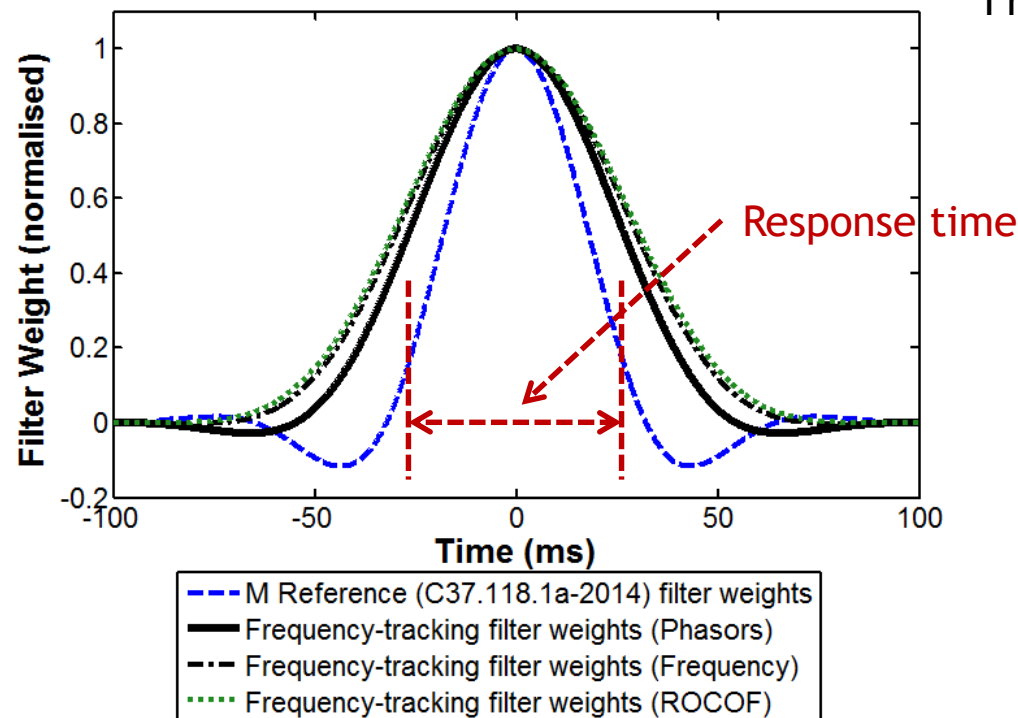
- M Reference (C37.118.1a-2014) filter response envelope
- Frequency-tracking filter response envelope (Phasors)
- · - Frequency-tracking filter response envelope (Frequency)
- Frequency-tracking filter response envelope (ROCOF)

Cascaded boxcar filters example, $f_0=50$ Hz, $F_S=50$ Hz

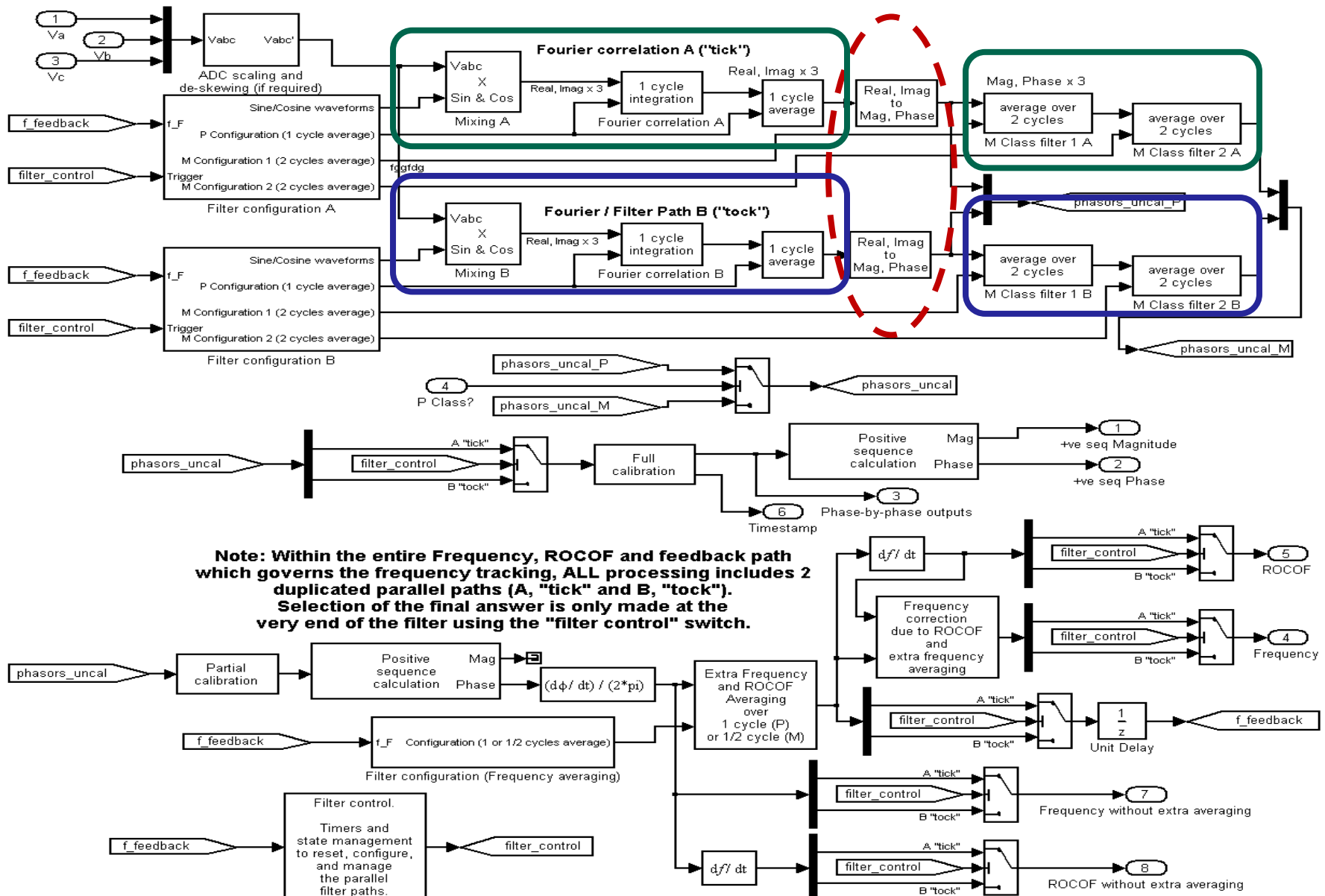


←----- Primary filter ----->
10 cycles, ~200ms at $f=50$ Hz
Latency ~5 cycles, ~100ms at $f=50$ Hz

Additional
Frequency (and ROCOF)
filtering



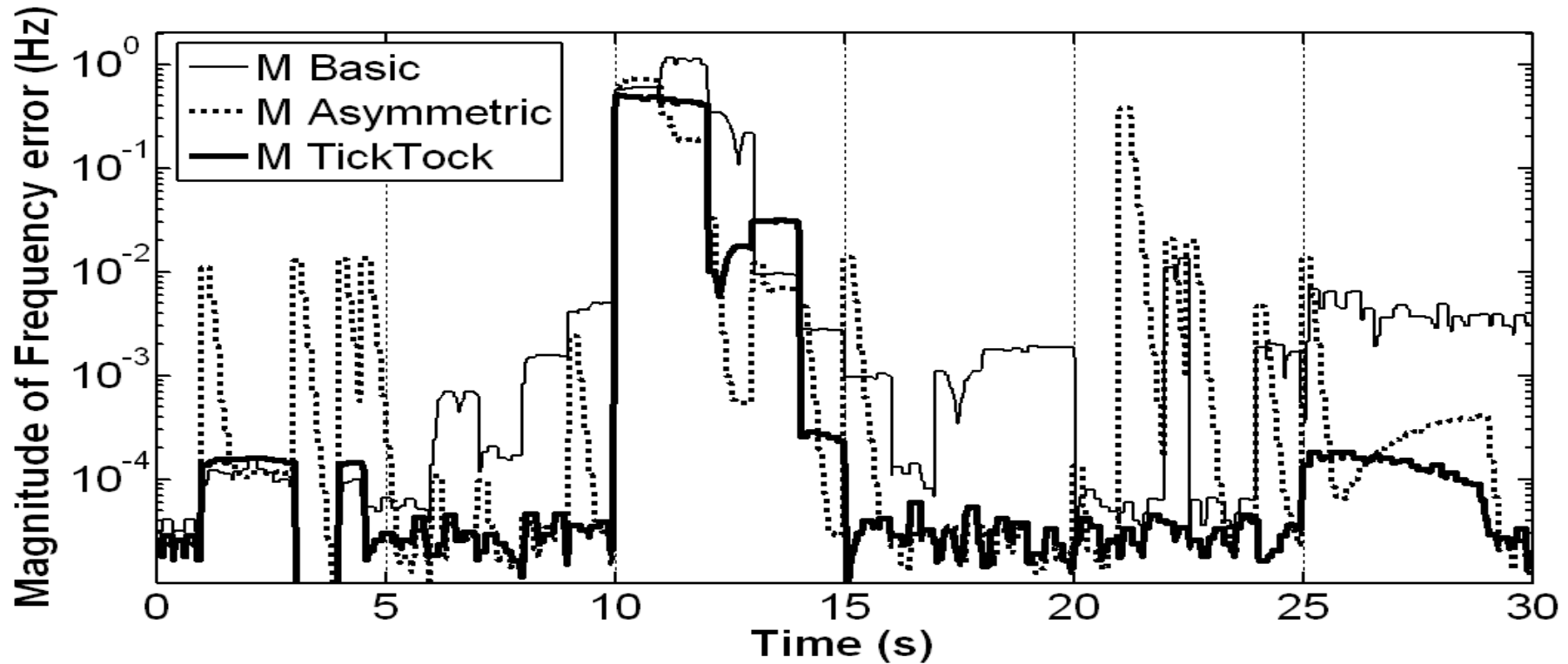
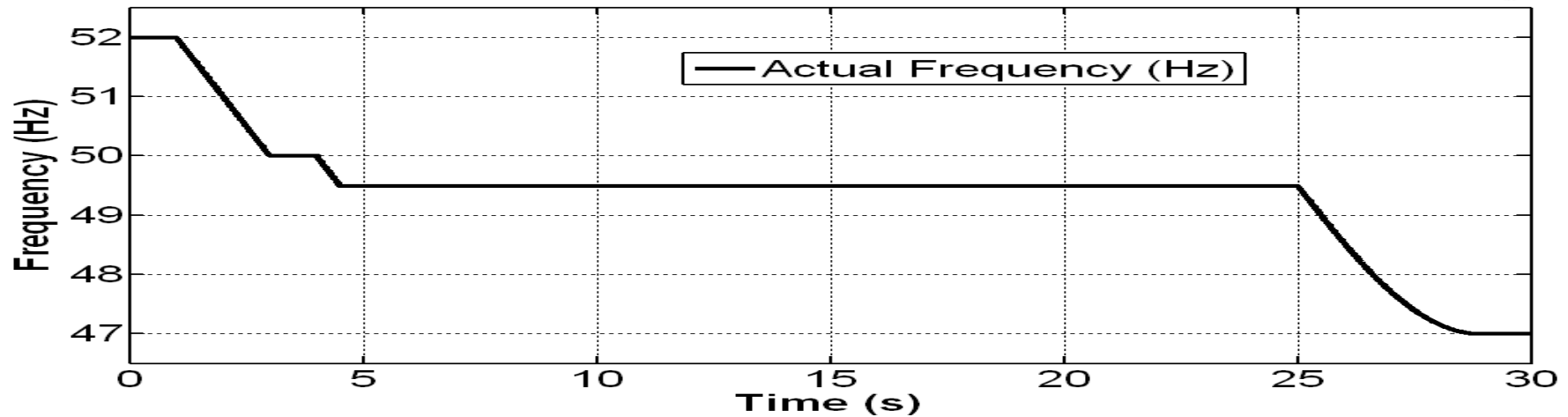
Example software architecture



Code execution speed

- 30-60 μ s Typical execution time per frame for M class PMU (Motorola MVME5500). Supports >10kHz reporting.
- Calculation rate does NOT increase for longer-window (lower reporting rate) devices, as long as the NUMBER of cascaded boxcar filter sections is kept constant.
 - But fast-access memory requirement does (\propto Window length).
- Can easily be extended to “Harmonic PMU” applications.
 - # Calculations expand $\propto N$ harmonics, memory expands $\propto N$ harmonics and \propto Window length
- Compare with
 - Least Squares and “TFT” algorithms, # calculations proportional to window length
 - FFT algorithms for harmonic PMUs, # calculations proportional to (window length)*log(window length)
 - Kalman filter methods, # calculations proportional to the number of filter zeros squared (matrix multiplications).

Non-standard tests and real-world conditions



Unfinished work - Increased fault tolerance for frequency and ROCOF - 27th August 2013 example – P class



Power outage in Glasgow after worker hits live cable



The worker was injured after making contact with a live cable on a building site in Allan Glen Place

A worker has been injured after making contact with a live cable at a building site in Glasgow city centre.

Police Scotland said there was a short power outage in the north of the city following the incident at Allen Glen Place at about 12:00 on Tuesday.

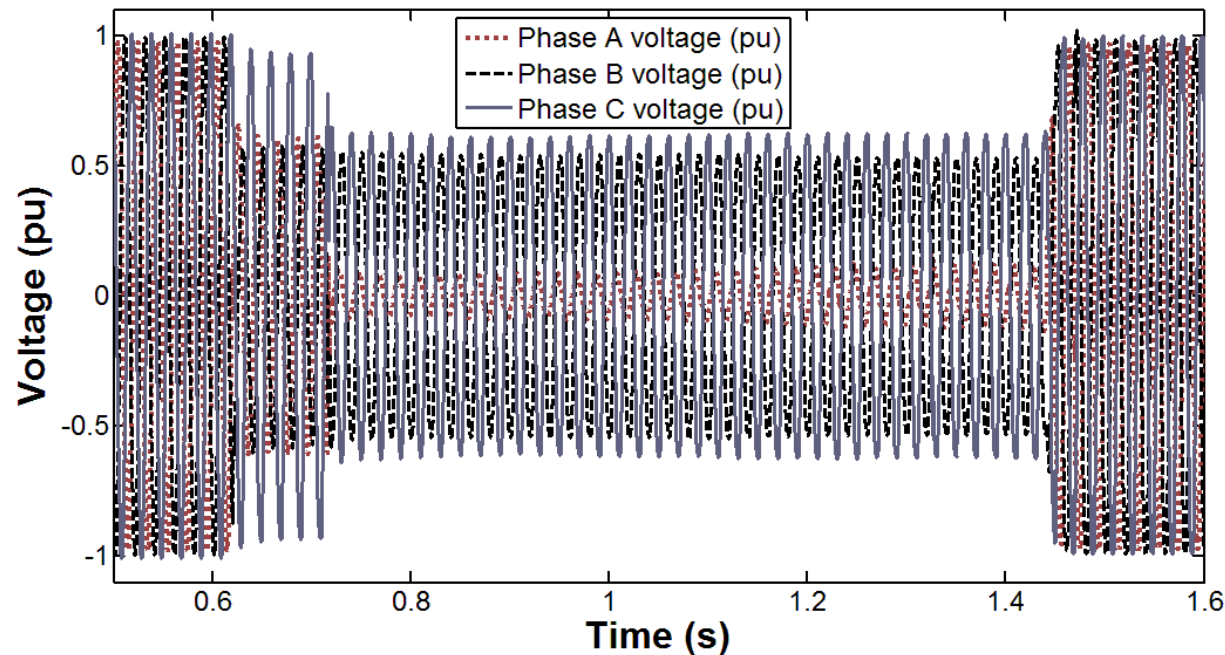
The injured man was taken to nearby Glasgow Royal Infirmary. Details of his condition are not yet known.

Emergency services remain at the scene. The incident has been reported to the Health and Safety Executive.

Scottish Power officials are also at the scene.

It is understood that people in the area reported hearing a "loud bang and explosion" when the incident occurred.

The power supply was restored a short time later.



Unfinished work - Increased fault tolerance for frequency and ROCOF - 27th August 2013 example – P class



27 August 2013 Last updated at 13:41



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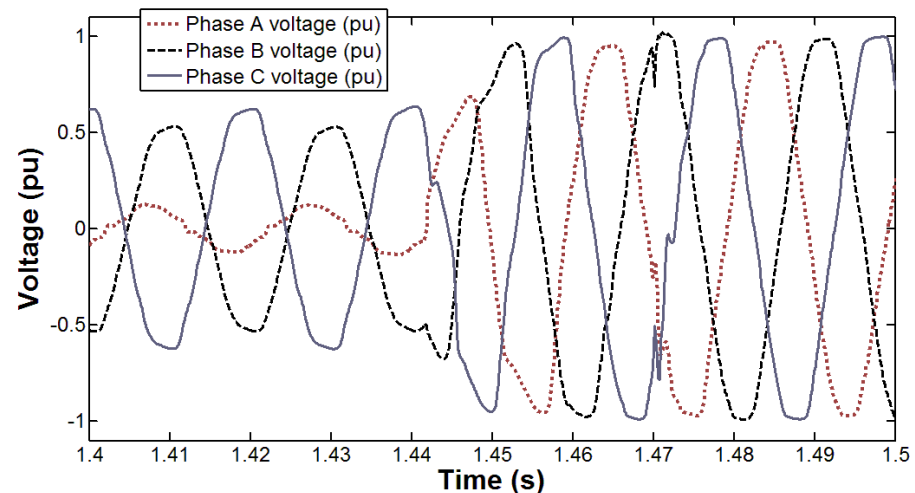
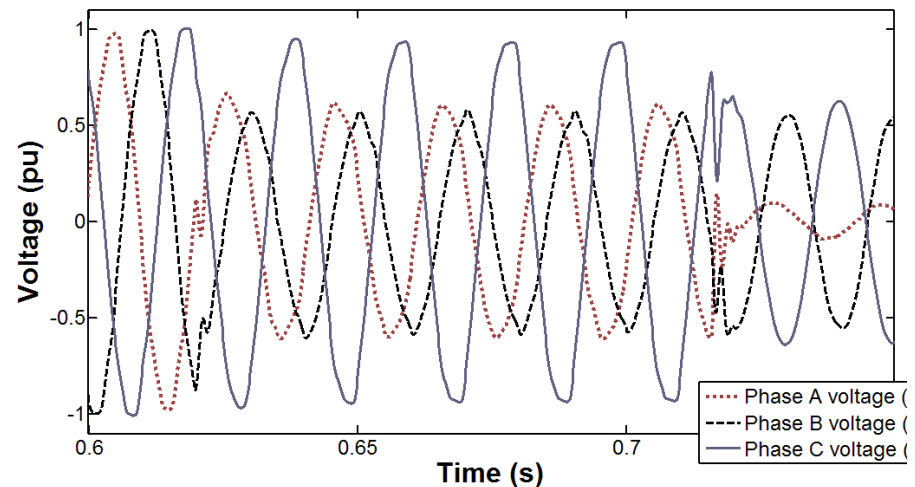
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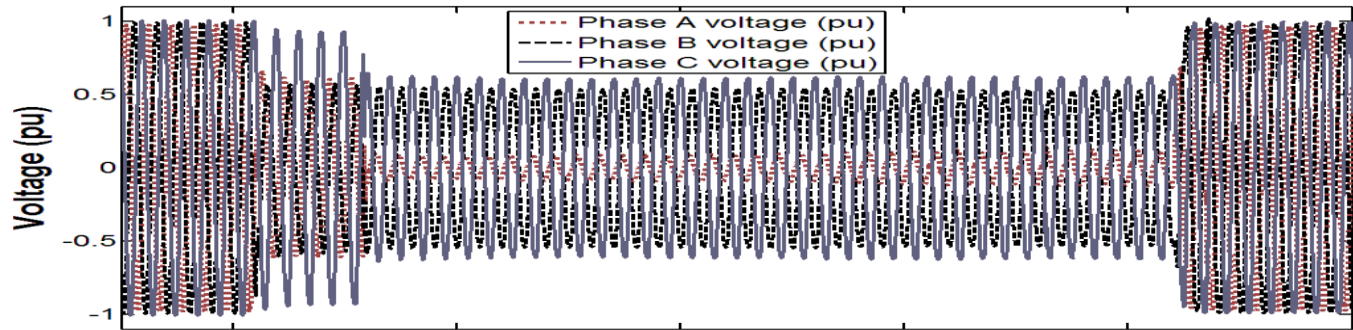
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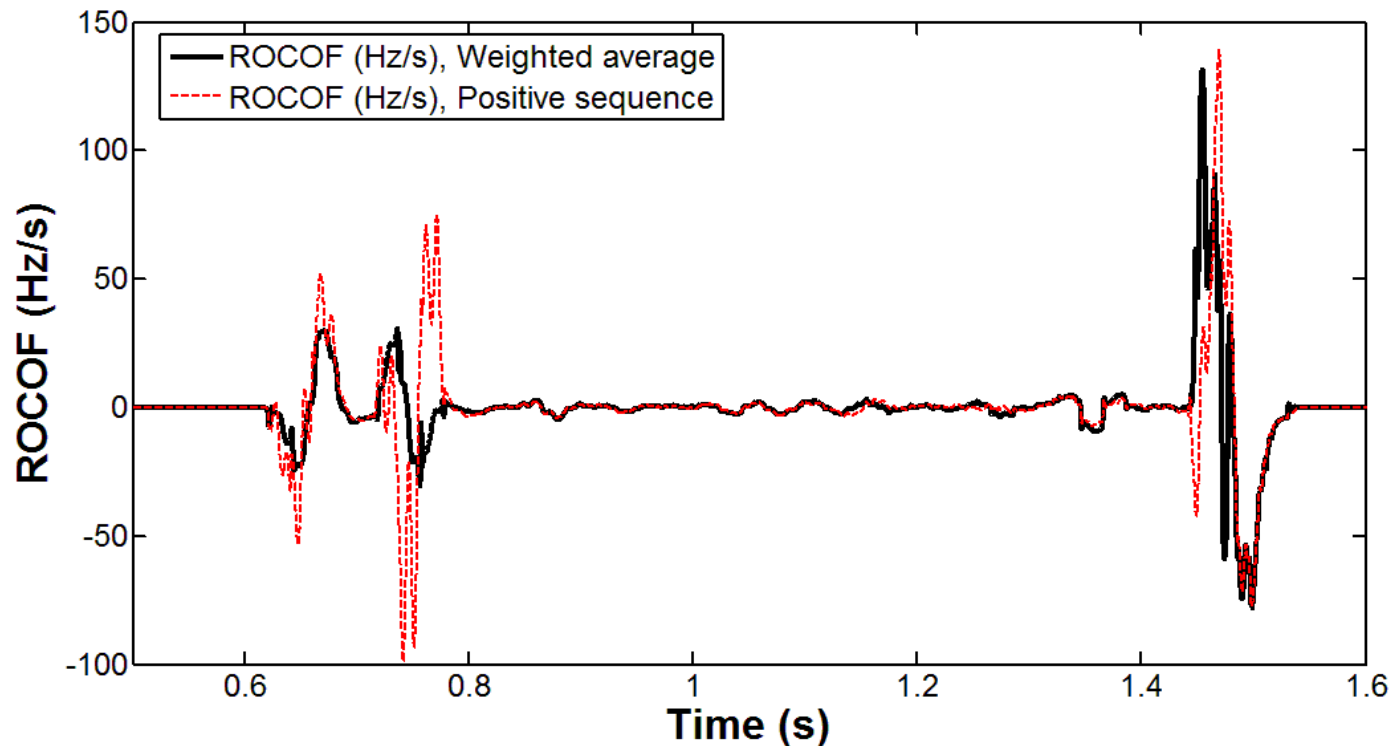
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Future considerations/work:

- Implement in hardware!
- Continuing input to standards development.
- Accurate revenue metering.
- Synchronised Power Quality assessment and PQ “metering”!
- Combinations of adaptive and fixed boxcars to provide “Uniform Aggregated Weighting” (Welch’s method) via repeated windows at fixed (i.e. 20ms) intervals, while also providing adaptive-zero-placement for off-nominal frequency.
- Integrating PMU algorithms within HVDC controllers?
- Aggregation of PMU ROCOF data across a geographically wide network to determine “system ROCOF” and required “inertial” responses.
 - “Enhanced Frequency Control Capability (EFCC)” with National Grid, Alstom, Belectric, Centrica, Flextricity & University of Manchester.

END